

**Izomer  $K^\pi = 8^-$  w  $^{132}\text{Ce}$ .**  
**Wpływ nieosiowego kształtu jądra na**  
**osłabienie czystości liczby kwantowej K.**  
**Dowód eksperymentalny?**

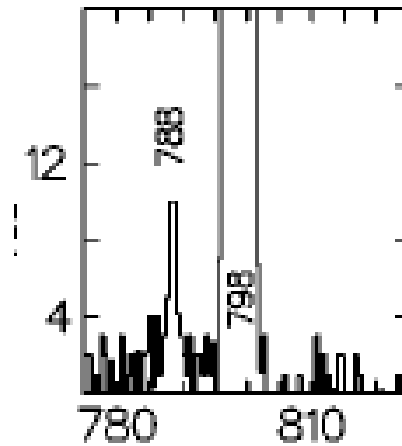
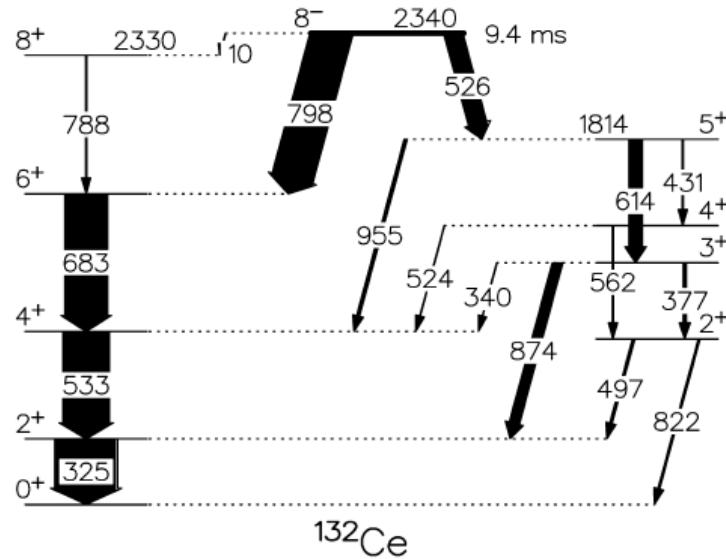
Julian Srebrny (ŚLCJ UW)

Seminarium Środowiskowe Fizyki Jądrowej 24 marca 2010

## Plan prezentacji

1. Dlaczego lubimy badać izomery?
2. Przypomnienie naszych prac o  $^{132}\text{Ce}$  z 2009 i 2001, kontynuacja Seminarium J. Perkowskiego z zeszłego roku.
3. Określenie liczby kwantowej K. Jak rozumieć czystość liczby kwantowej?
4. Trójosiowy rotor, model D-F - **zmieszanie K, w tym K=4.**  
Czy to tłumaczy  **$B(E3;8^- \rightarrow 5^+)$**  i  **$B(E3;8^- \rightarrow 6^+)$**  ?
5. Przejścia E1 jako miara domieszek S-band do GSB w  $^{132}\text{Ce}$
6. Wzbudzenia kulombowskie z  $K=0$  do  $K=16$  w  $^{178}\text{Hf}$ , ten sam mechanizm jak dla E1 w  $^{132}\text{Ce}$
7. Podsumowanie: różne mechanizmy rozpadu izomeru K





Ge – Ge

PHYSICAL REVIEW C, VOLUME 63, 034302

**Investigation of the  $K^\pi = 8^-$  isomer in  $^{132}\text{Ce}$**

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 (Received 6 July 2000; published 31 January 2001)

**Z = 54..... 64**

**N = 74 prolate(od Xe..... Dy)**

$$\frac{7}{2}^+ [404] \otimes \frac{9}{2}^- [514]$$

**R. Moore et al. moment magnetyczny  $^{130}\text{Ba}$**

**Physics Letters B 547 (2002) 200–204**

***Eur. Phys. J. A 42, 379–382 (2009)***

Regular Article – Experimental Physics

**Absolute E3 and M2 transition probabilities for the  
electromagnetic decay of the  $I^\pi = K^\pi = 8^-$  isomeric state in  $^{132}\text{Ce}$**

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M. Kisielinski<sup>2,4</sup>, A. Korman<sup>4</sup>, M. Kowalczyk<sup>2,3</sup>, J. Kownacki<sup>2</sup>, A. Król<sup>1</sup>, J. Marganiec<sup>1,9</sup>,  
J. Mierzejewski<sup>2,3</sup>, T. Morek<sup>3</sup>, K. Sobczak<sup>1,8</sup>, H. Trzaska<sup>5,6</sup>, and M. Zielinska<sup>2</sup>

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***"Workshop on Nuclear Isomers: Structure and Applications"***

***19 - 21 May 2010 at the University of Surrey, Guildford, UK***

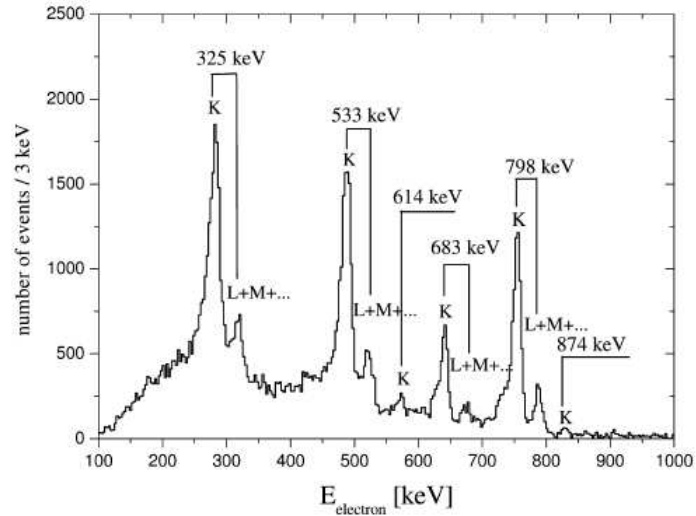


Fig. 3. Summed electron spectrum observed in coincidence with the 325, 533 and 683 keV gamma-ray transitions.

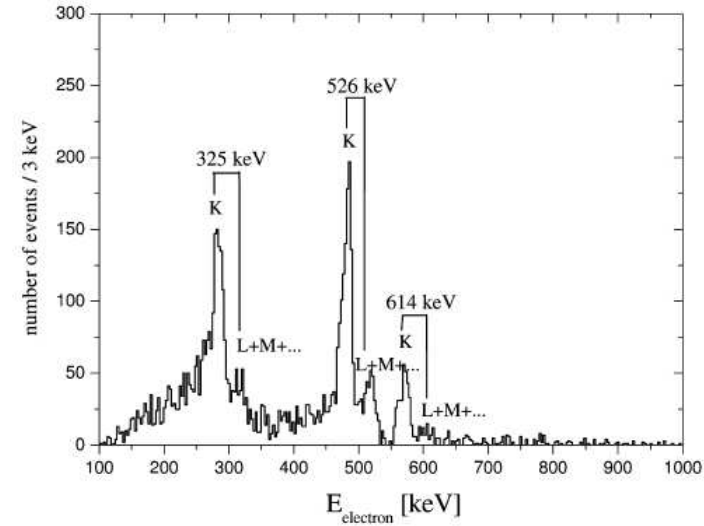
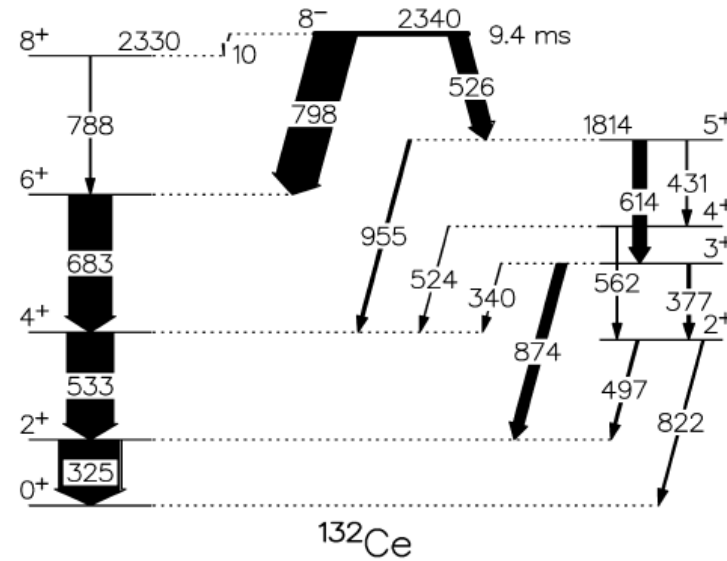
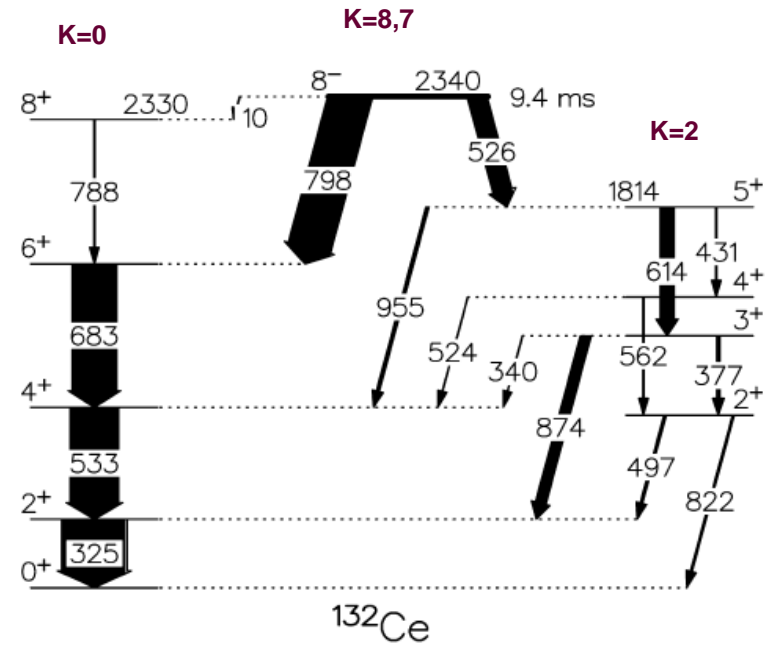
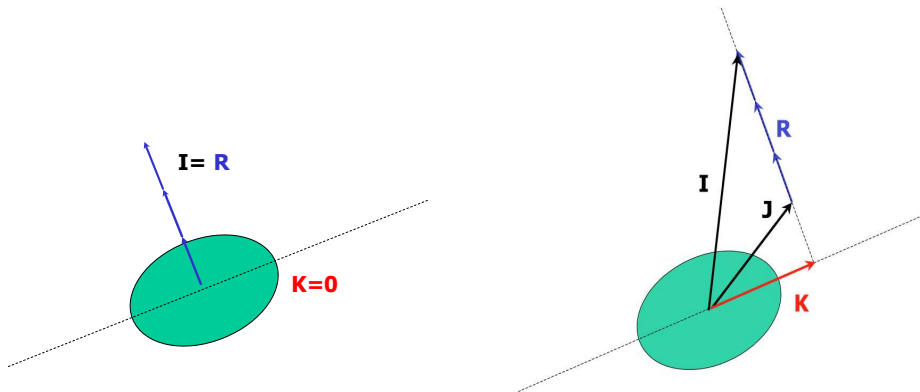


Fig. 4. Electron spectrum observed in coincidence with the 874 keV gamma-ray transition.



Określenie multipułowości 614 keV(E2), 526 keV(E3) i 798 keV( 65% E3 + 35% M2)

Określenie spinów i parzystości 5+ i 8-



## Wzbronienie K

Stopień wzbronienia:  $\nu = \Delta K - \lambda$

osłabienie przejść  $\Delta K > \lambda$  o rzędy wielkości

$$F = T_{1/2}^P / T_{1/2}^W$$

$$f_\nu = F^{1/\nu}$$

## DF **trójosiowy sztywny rotor (najprostszy model z $\gamma$ )**

### Davydov-Filippov Code.

The DF code is designed to calculate energies of collective states (up to spin 30) and reduced matrix elements of E2 transitions in even-even nuclei.

Calculations based of the Davidov-Filippov model of rigid asymmetric rotor [1] can be performed with the E2 operator :

$$M_{E2}(\beta, \cos(\gamma))$$

or

$$M_{E2}(\beta, \cos(\gamma), \beta^2, \cos(2\gamma))$$

An input file for the FAUST code can be created as an option.

#### History of versions:

1992 – ver.1.

2007 – ver. 2. Variable moment of inertia [2] was added.

#### Downloads:

[kdf2.pas](#)

the source code written in Borland Turbo-Pascal

[kdf2.exe](#)

the [executable](#) file working under control of DOS or Microsoft Windows operating systems

[df\\_manual.pdf](#)

the manual.

#### References:

[1] A.S. Davydov and G.F. Filippov, *Nucl. Phys.* **8** (1958) 237.

[2] M. A. J. Mariscotti, G. Scharff-Goldhaber, and B. Buck, *Phys.Rev.* **178** (1969) 1864.

Last update: 15/05/2008

[Paweł J. Napiorkowski](#)



PROGRAM DAVYDOV-FILIPOV

Z = 58 A = 132 EN( 2, 1) = 300.0 keV beta= 0.2500 gamma = 25.00 [deg]

Level	Energy [keV]	
0( 1)	0.00	0.0000
[ 0]	1.00000	
2( 1)	300.00	1.0000
[ 0]	<b>0.97396</b>	[ 2] <b>0.22670</b>
2( 2)	722.33	2.4078
[ 0]	<b>-0.22670</b>	[ 2] <b>0.97396</b>
3( 1)	1022.33	3.4078
[ 2]	1.00000	
4( 1)	850.82	2.8361
[ 0]	<b>0.85163</b>	[ 2] <b>0.52239</b> [ 4] <b>0.04283</b>
4( 2)	1653.85	5.5128
[ 0]	-0.52323	[ 2] 0.84246 [ 4] 0.12846
4( 3)	2606.97	8.6899
[ 0]	0.03102	[ 2]-0.13181 [ 4] 0.99079
5( 1)	1922.33	6.4078
[ 2]	<b>0.97396</b>	[ 4] <b>0.22670</b>
5( 2)	3189.31	10.6310
[ 2]	-0.22670	[ 4] 0.97396
6( 1)	1602.59	5.3420
[ 0]	0.76204	[ 2] 0.63424 [ 4] 0.13029 [ 6] 0.00702
6( 2)	3077.22	10.2574
[ 0]	-0.61930	[ 2] 0.65509 [ 4] 0.43127 [ 6] 0.03649
6( 3)	3944.77	13.1492
[ 0]	0.18905	[ 2]-0.41020 [ 4] 0.88504 [ 6] 0.11270
7( 1)	3091.74	10.3058
[ 2]	0.90763	[ 4] 0.41658 [ 6] 0.05165
8( 1)	2565.78	8.5526
[ 0]	0.70567	[ 2] 0.67610 [ 4] 0.21006 [ 6] 0.02815 [ 8] 0.00113

Gamma=27.5

I=5+

K= [2] 88%, K= [4] 12.3%

I=6+

K= [0] 51%, K= [2] 45%, K= [4] 3.6%, K= [6] 0.02%

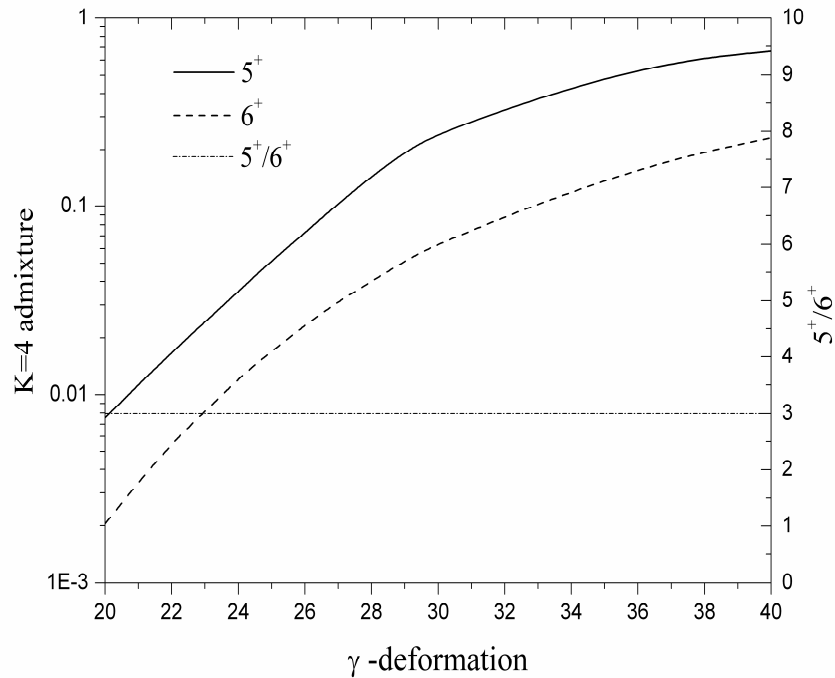
gamma=24

I=5+

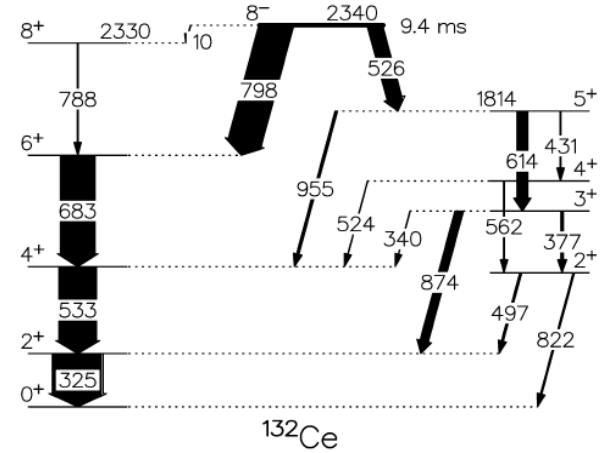
K= [2] 96%, K= [4] 3.6%

I=6+

K= [0] 61%, K= [2] 37%, K= [4] 1.20%, K=[6] 0.003%



K=0                      K=8,7                      K=2



$$B(E3; 8^- \rightarrow 5^+) / B(E3; 8^- \rightarrow 6^+) = 12(2)$$

miara domieszki K=4 w obu stanach

$$\nu = \Delta K - \lambda$$

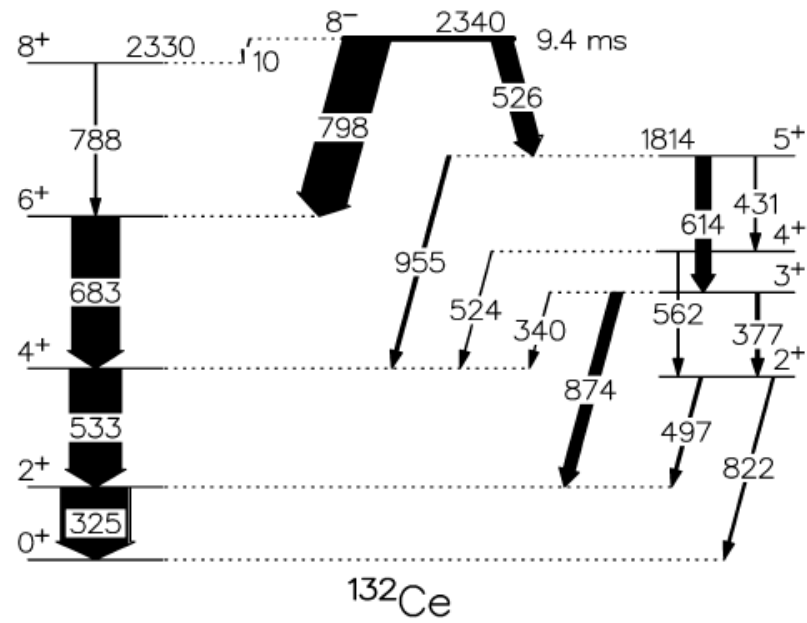
$$\nu = (7 - 4) - 3 = 0 \quad \text{brak wzbronienia}$$

$$B(E3; 8^- \rightarrow 5^+) / B(E3; 8^- \rightarrow 6^+) =$$

$$[\langle 8 \ 7 \ 3 \ -3 | 5 \ 4 \rangle / \langle 8 \ 7 \ 3 \ -3 | 6 \ 4 \rangle]^2 \times [a(5^+) / a(6^+)]$$

Exp.:  $a(5^+) / a(6^+) = 12(2) / 1.15 = 10(2)$

D-F theory:  $a(5^+; \gamma = 27.5) / a(6^+; \gamma = 24) = 10.2$



**Exp.:**  $a(5+)/a(6+) = 12(2) / 1.15 = 10(2)$

**D-F theory:**  $a(5+; \gamma = 27.5) / a(6+; \gamma = 24) = 10.2$

$\Delta\gamma = 3.5 \pm 1.0^\circ$

$$B(E1; 8^- \rightarrow 8^+) \quad f_7$$

A.M. Bruce, A.P. Byrne, G.D. Dracoulis, W. Gelletly, T. Kibedi, F.G. Kondev, C.S. Purry, P.H. Regan, C. Thwaites, and P.M. Walker, Phys. Rev. C 55, 620 (1997).

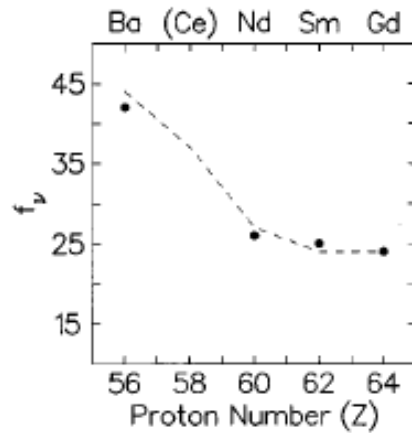


FIG. 3. Systematics of  $f_v$  values for observed  $E1$  decays from the  $K^\pi=8^-$  isomers in the  $N=74$  isotones. The line depicts the  $f_v$  values which are predicted using the band-mixing calculation outlined in Sec. III A.

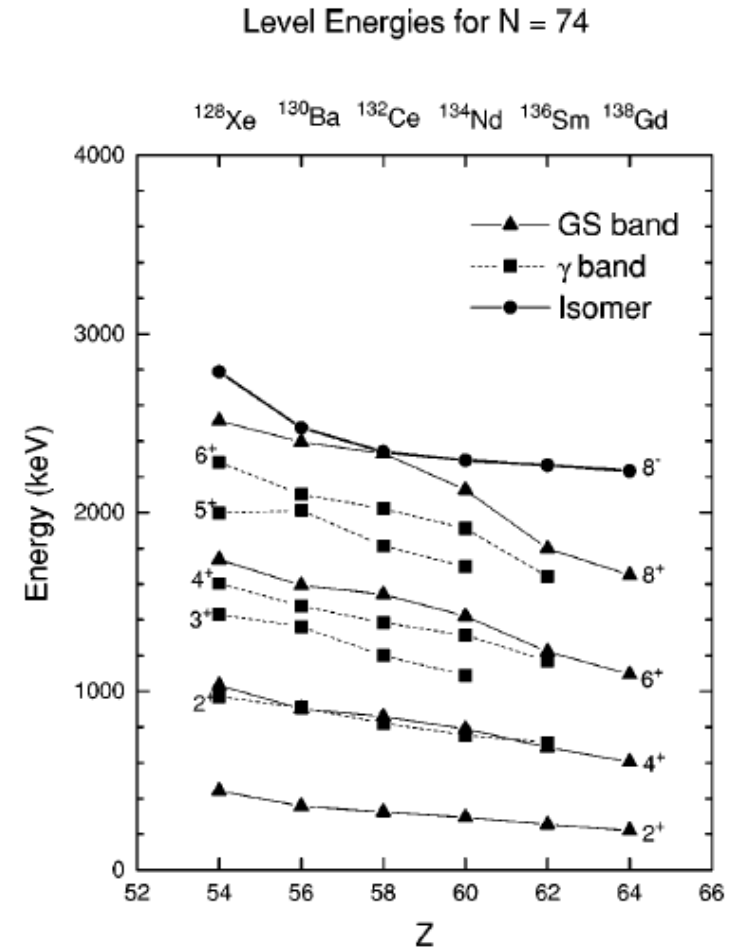


FIG. 5. Systematics of the excited levels with  $I \leq 8$  relevant for the discussion of the even-even  $N=74$  isotones.

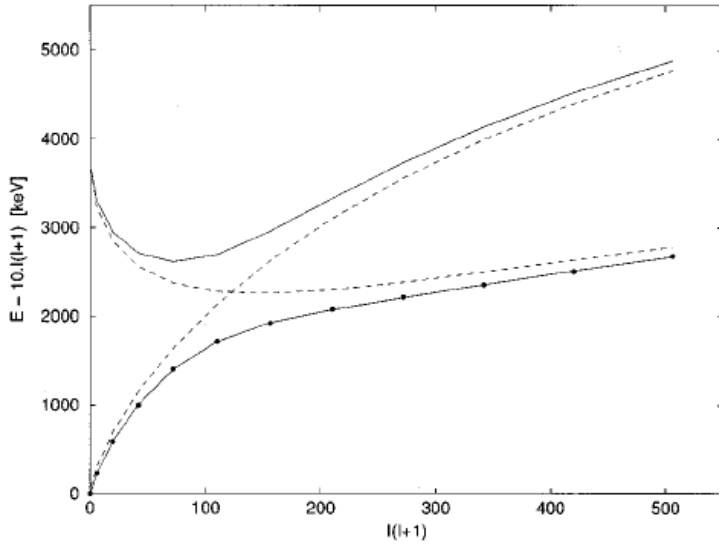


FIG. 5. The results of the two-band mixing calculation for  $^{134}\text{Nd}$ . The unperturbed bands are shown as dashed lines and the perturbed bands as solid lines. The dots represent the measured excitation energies of the states in the yrast band.

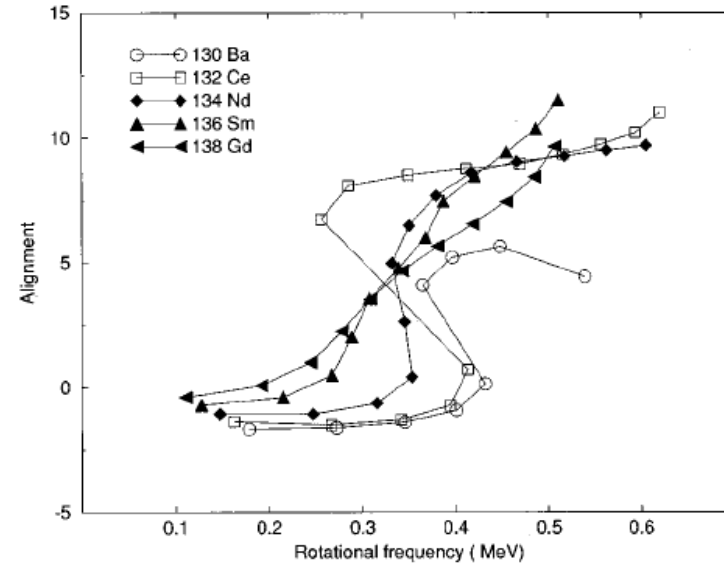


FIG. 4. Experimental alignments for  $^{130}\text{Ba}$ ,  $^{132}\text{Ce}$ ,  $^{134}\text{Nd}$ ,  $^{136}\text{Sm}$ , and  $^{138}\text{Gd}$ . Harris reference parameters of  $\mathcal{I}_0 = 17.0 \hbar^2 \text{ MeV}^{-1}$  and  $\mathcal{I}_1 = 25.0 \hbar^4 \text{ MeV}^{-3}$  have been used for all five nuclei.

A.M. Bruce, A.P. Byrne, G.D. Dracoulis, W. Gelletly, T. Kibedi, F.G. Kondev,  
 C.S. Purry, P.H. Regan, C. Thwaites, and P.M. Walker,  
 Phys. Rev. C **55**, 620 (1997)

## Spin dependence of $K$ mixing, strong configuration mixing, and electromagnetic properties of $^{178}\text{Hf}$

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(Received 16 October 2006; published 16 March 2007)

$^{178}\text{Hf}(^{136}\text{Xe}, ^{136}\text{Xe})^{178}\text{Hf}$  coulomb excitation

**Z=74**

**Ta (  $^{178}\text{Hf}$ ,  $^{178}\text{Hf}$  ) Ta** Coulomb excitation, activation experiment

Ten sam mechanizm powstawania domieszek wysokich  $K$  dla pasma o niskich  $K$ ,  
jak dla przejść  $E1$  w  $N=74$

**$^{178}\text{Hf}$   $Z=74$  COULEX  $z=0^+$**

A. B. HAYES *et al.*

PHYSICAL REVIEW C 75, 034308 (2007)

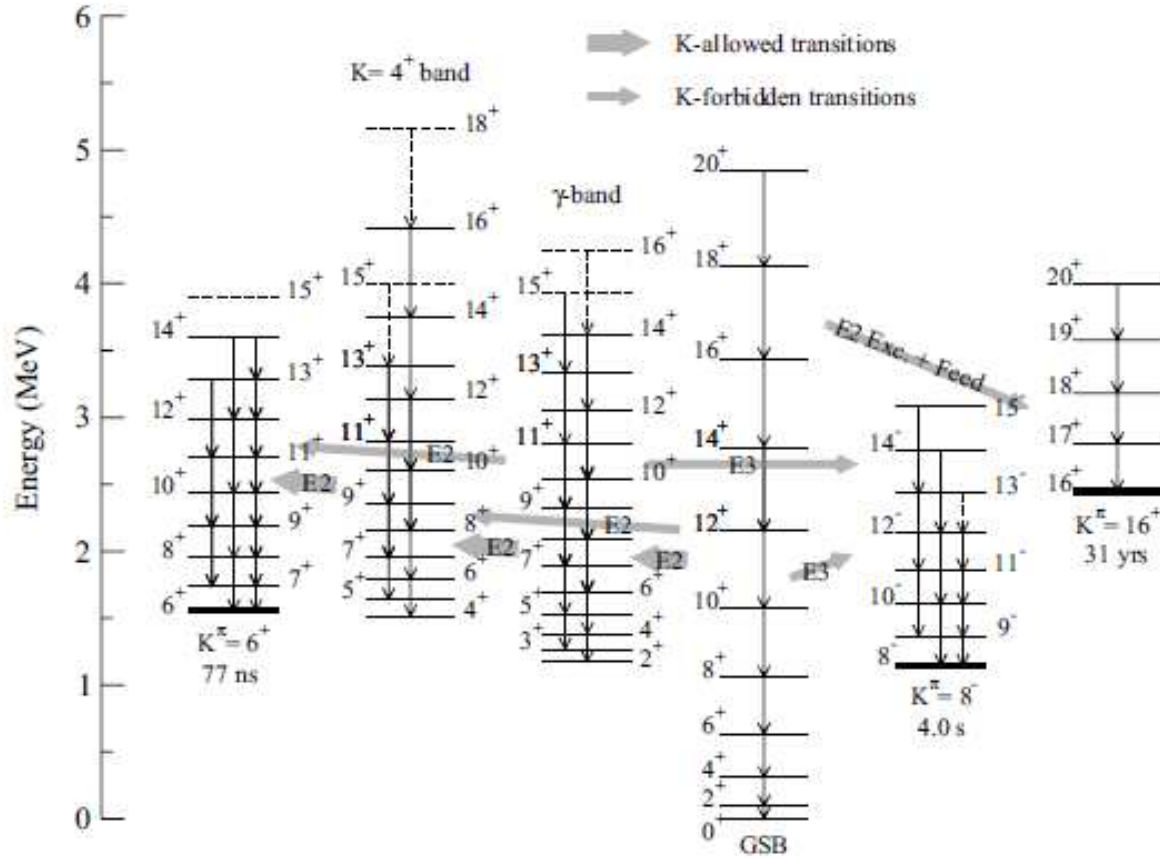


FIG. 18. A schematic representation of the population paths to the three isomer bands. The narrow and wide arrows represent band  $\rightarrow$  band transitions.

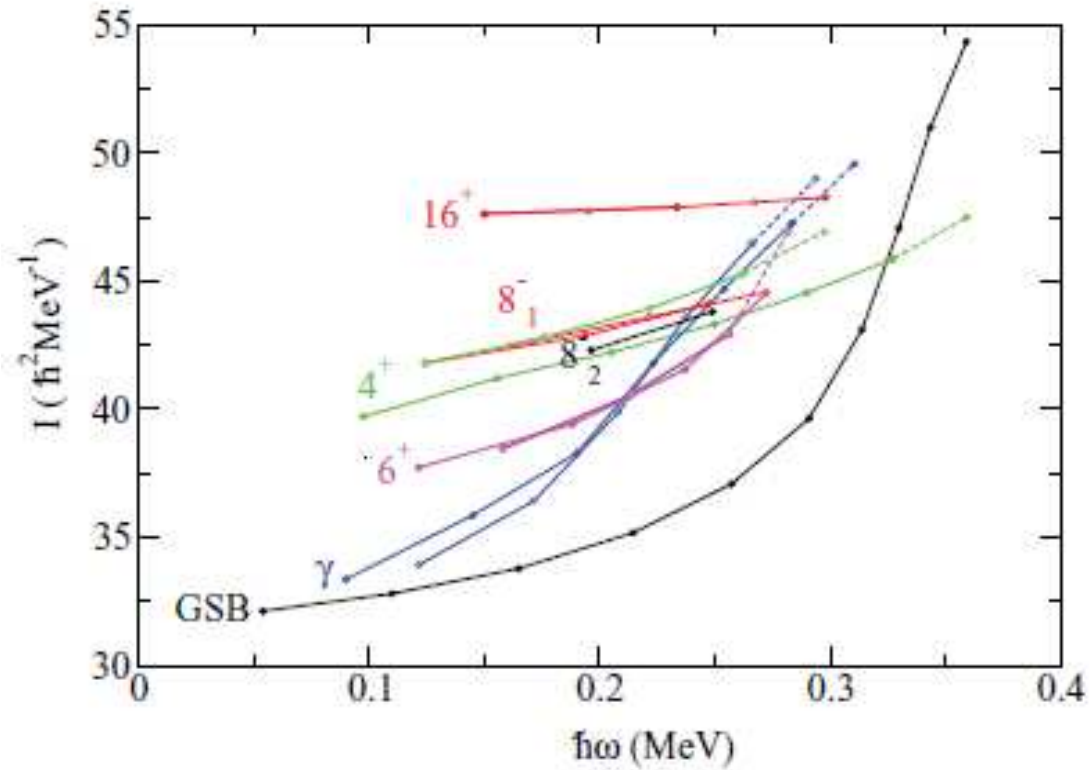


FIG. 35. (Color online) Measured moments of inertia of  $^{178}\text{Hf}$  rotational bands. Dashed lines connect to tentatively assigned

szybka zmiana momentu bezwładności dla pasm o niskim K - GSB,  $\gamma$   
 dla coraz większej rotacji stopniowe rozerwanie jednej pary, potem drugiej pary protonów  
 stałość momentu bezwładności dla pasm o wysokim K -  $16^+$ ,  $8^-$



SPIN DEPENDENCE OF  $K$  MIXING, STRONG ...

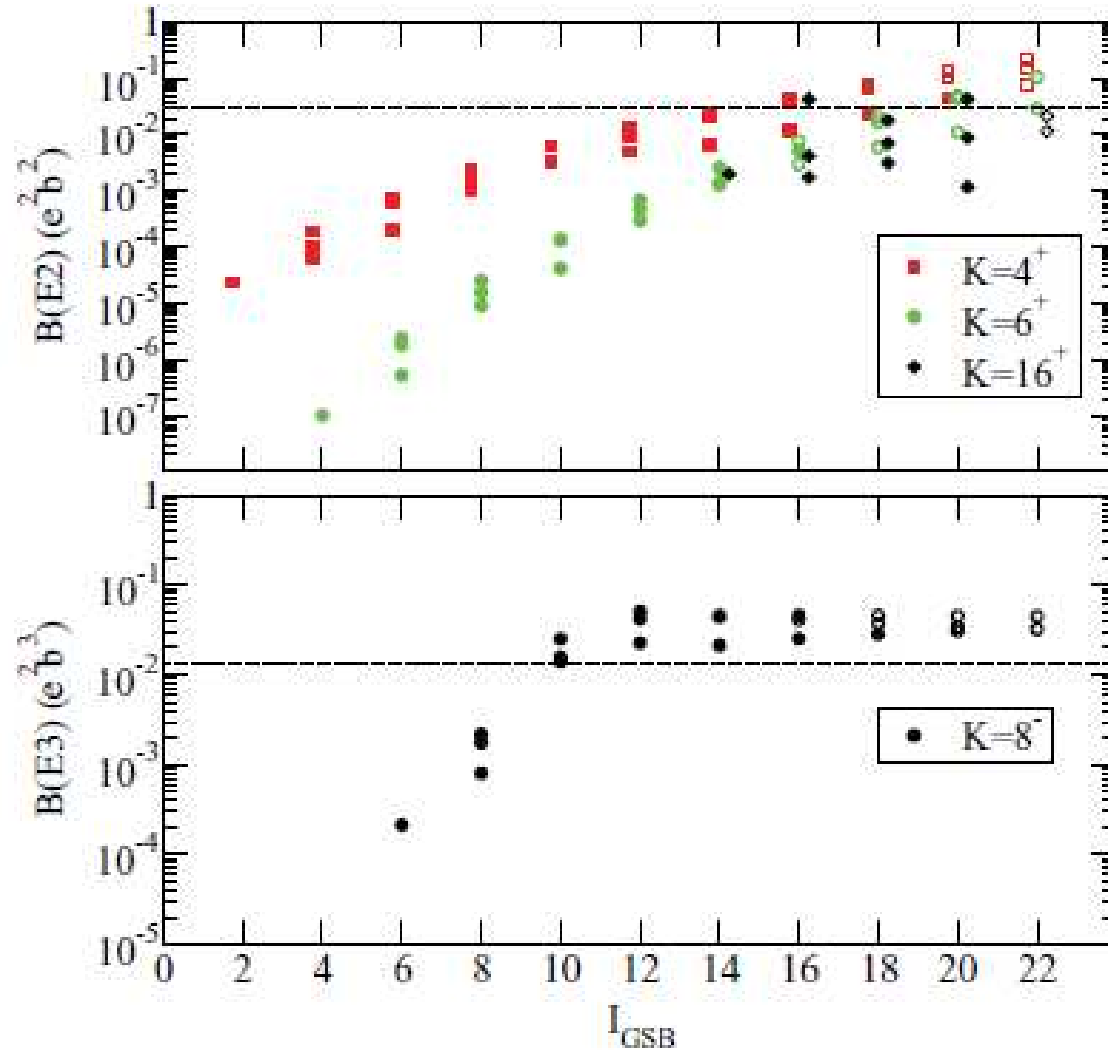


FIG. 33. (Color online) The three strongest reduced transition probabilities from each GSB level for  $\text{GSB} \rightarrow K^\pi$  transitions.  $\text{GSB} \rightarrow$

**$^{178}\text{Hf}$  Z=74 COULEX z 0<sup>+</sup>**

A. B. HAYES *et al.*

PHYSICAL REVIEW C 75, 034308 (2007)

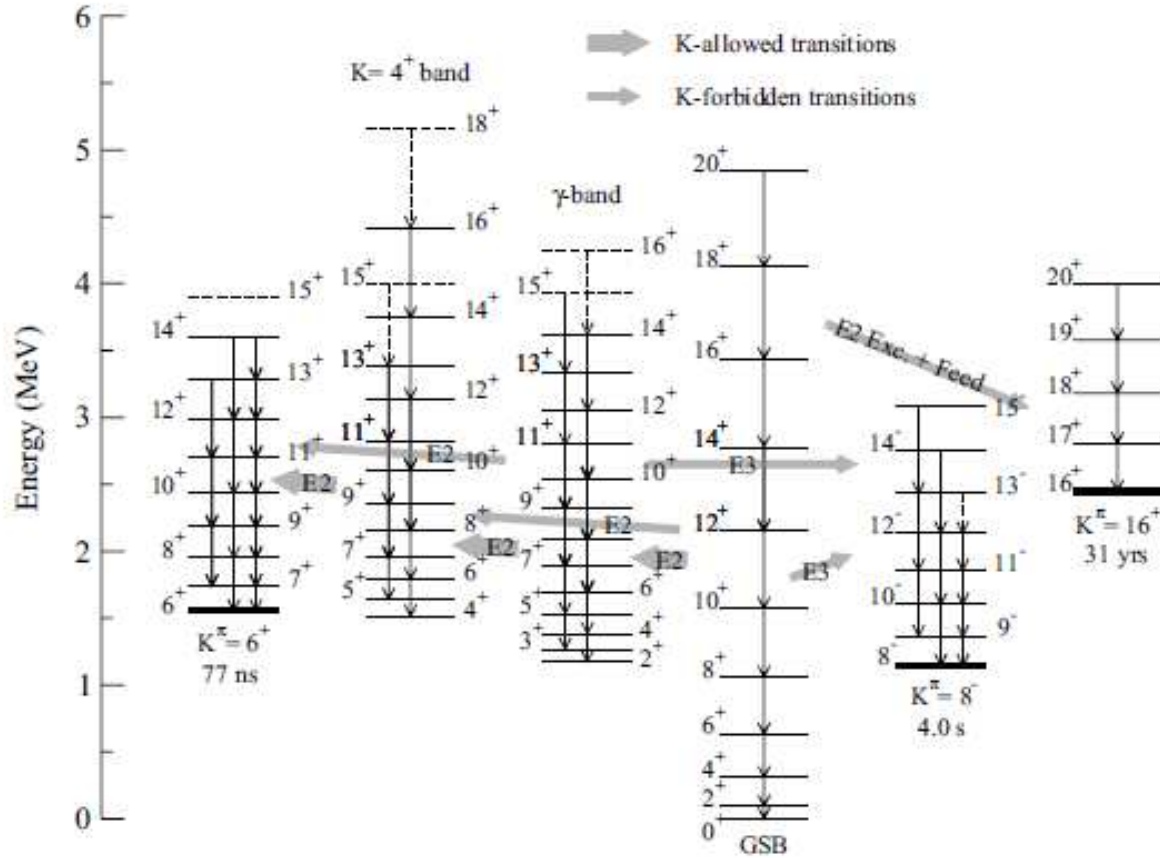


FIG. 18. A schematic representation of the population paths to the three isomer bands. The narrow and wide arrows represent band → band transitions.

## SUMMARY

1. Stosunki  $B(E3; 8^- \rightarrow 5^+, 6^+)$  miarą domieszek  $a(K=4)$ .  
Zaś  $a(K=4)$  miarą deformacji trójosiowej.  
Wyniki pomiarów konsyistentne z  $\Delta\gamma = 3.5 \pm 1.0$
2. Dla  $B(E1; 8^- \rightarrow 8^+)$  mechanizm naruszenia czystości liczby kwantowej  $K$  taki sam w  $^{178}\text{Hf}$  i  $^{132}\text{Ce}$ : symetria osiowa i domieszki wysokich  $K$  do pasma o niskim  $K$ : Coriolis alignment.
3. Wagi obu mechanizmów możliwe przez porównanie rozkładów  $K$  f. falowych poszczególnych stanów.

Assuming  $K=0$  for the ground state band,  
 and 99.46% ground and 0.53% S - for the 6+ in  
 $^{132}\text{Ce}$ ,  
 we get the following distribution:

GSB - S	K	D-F( $\gamma=25$ )	D-F/yours
99.55%	0	58%	0.58
0.17	1		
0.13	2	40	313
0.08	3		
0.04	4	1.7	43
0.016	5		
0.005	6	0.005	1
0.0012			
0.0002			
2.03E-05			
1.02E-06			

which does add up to 100% in both cases.