

# Gamow-Teller transitions: vivid nuclear weak process in the Universe

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GT : Important weak response, simple  $\sigma\tau$  operator

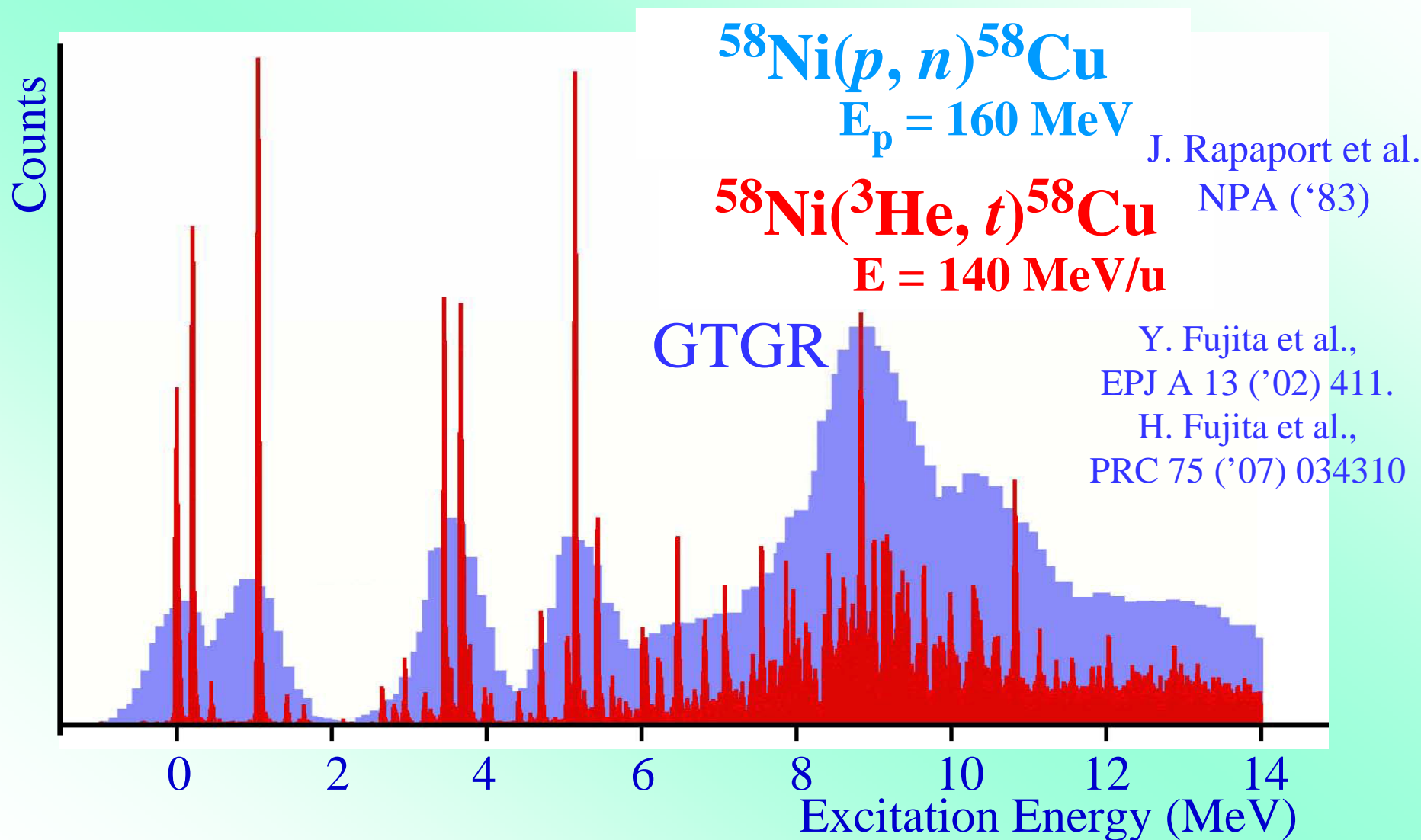
- ✧ Good Probe to Study the Key Part of the Nuclear Structure
- ✧ Astrophysical Interest

$\beta$  decay : absolute  $B(\text{GT})$ , limited to low-lying state

$(^3\text{He}, t)$  reaction : relative  $B(\text{GT})$ , Highly Excited States

\*\* both are important for the GT studies!

# Comparison of (p, n) and ( $^3\text{He}, t$ ) $0^\circ$ spectra



Neptune driving Waves  
波を操る海神ネプチューン

Neptune=弱い相互作用  
(weak interaction)



Powerful Waves=強い相互作用  
(strong interaction)

Neptune and the waves, or "steeds," he rides.

— Walter Crane, 1892

# Crucial Weak Processes

during the  
Core Collapse

mainly by  $\tau$  &  $\sigma\tau$

**Gamow-Teller (GT)  
transitions**

Langanke & Martinez-Pinedo  
Rev.Mod.Phys.75('04)819

Balantekin & Fuller  
J.Phys.G 29('03)2513

$$p + e^- \rightleftharpoons n + \nu_e,$$

$$n + e^+ \rightleftharpoons p + \bar{\nu}_e.$$

(A,Z)=nuclei in the  
Fe, Ni region

$$(A, Z) + e^- \rightleftharpoons (A, Z-1) + \nu_e,$$

$$(A, Z) + e^+ \rightleftharpoons (A, Z+1) + \bar{\nu}_e.$$

$$\nu + N \rightleftharpoons \nu + N$$

$$N +$$

**$\beta$ -decay, e-capture,  
 $\nu$ -induced reactions**

$$\nu + (A, Z) \rightleftharpoons \nu + (A, Z),$$

$$\nu + e^\pm \rightleftharpoons \nu + e^\pm,$$

$$\nu + (A, Z) \rightleftharpoons \nu + (A, Z)^*,$$

$$e^+ + e^- \rightleftharpoons \nu + \bar{\nu},$$

$$(A, Z)^* \rightleftharpoons (A, Z) + \nu + \bar{\nu}.$$

**\*\* Nuclear Excitations \*\***  
by  
Charge Exchange Reaction  
and  $\beta$ -Decay

**Study of Weak Response of Nuclei  
by means of  
Strong Interaction !?**

# $\beta$ -decay & Nuclear Reaction

$$*\beta\text{-decay GT tra. rate} = \frac{1}{t_{1/2}} = f \frac{\lambda^2}{K} \boxed{B(\text{GT})}$$

$B(\text{GT})$  : reduced GT transition strength  
 $\propto (\text{matrix element})^2$

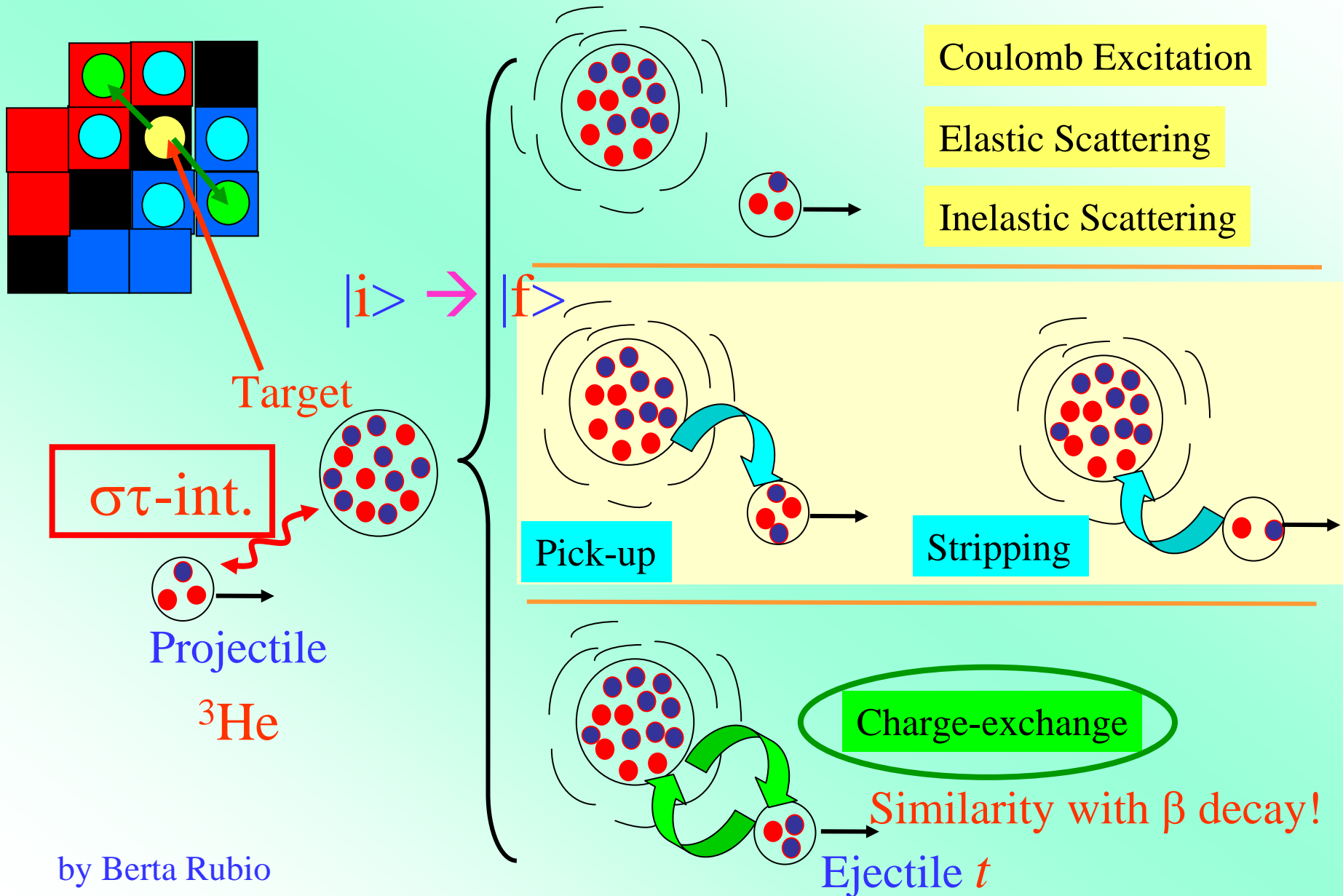
\*Nuclear (CE) reaction rate (cross-section)  
= reaction mechanism

$$\boxed{\begin{array}{l} \text{⊗ operator} \\ \text{⊗ structure} \end{array}} = (\text{matrix element})^2$$

A simple reaction mechanism should be achieved !

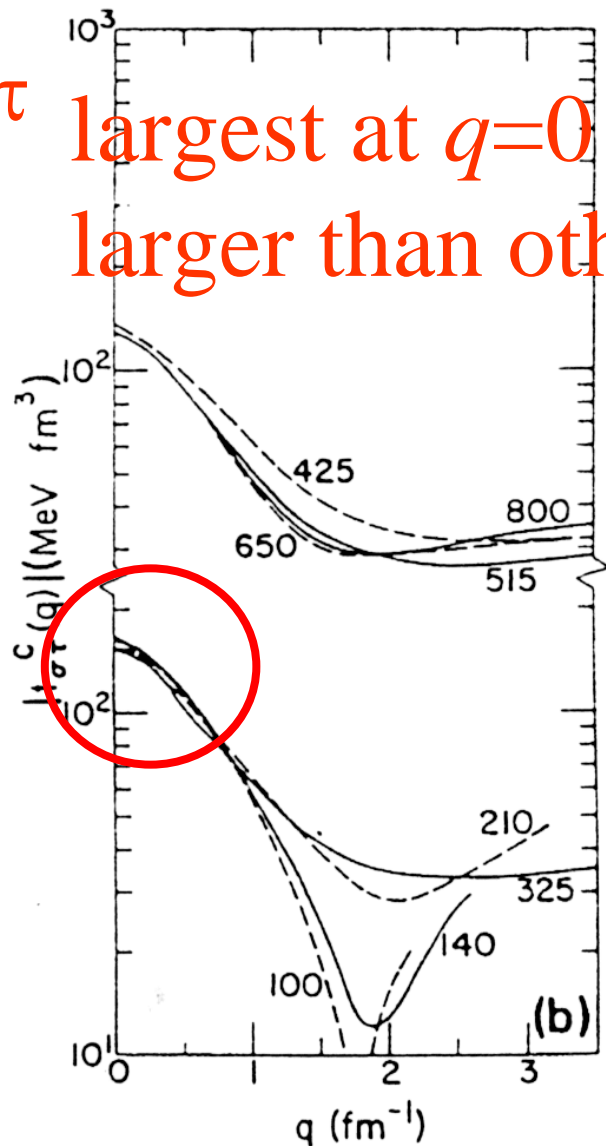
→ we have to go to high incoming energy

# Direct Reactions with Light Projectiles

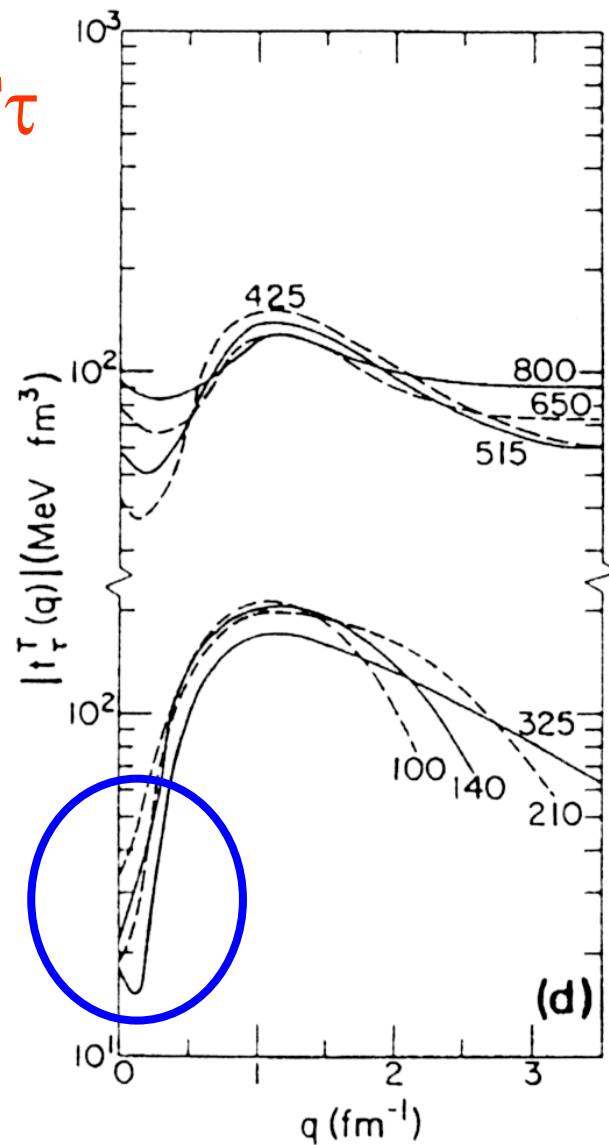


# N.-N. Int. : $\sigma\tau$ & Tensor- $\tau$ $q$ -dependence

$\sigma\tau$  largest at  $q=0$  !  
larger than others !



$T\tau$

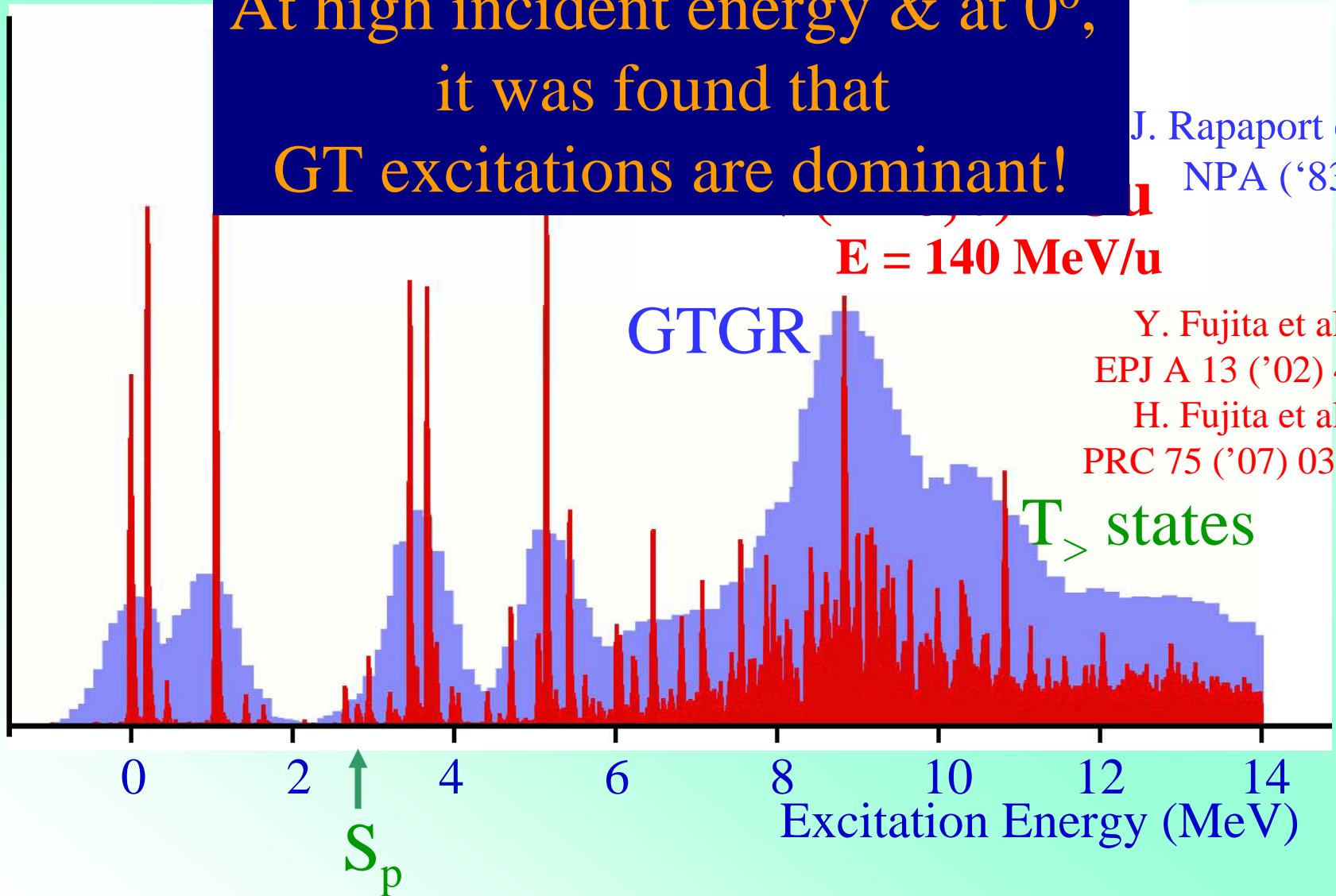




# Comparison of (p, n) and (<sup>3</sup>He, t) 0° spectra

At high incident energy & at 0°,  
it was found that  
GT excitations are dominant!

Counts



J. Rapaport et al.,  
NPA ('83)

**E = 140 MeV/u**

GTGR

Y. Fujita et al.,  
EPJ A 13 ('02) 411.  
H. Fujita et al.,  
PRC 75 ('07) 034310

$T_{>}$  states

0

2

4

6

8

10

12

14

Excitation Energy (MeV)

$S_p$

# $\beta$ -decay & Nuclear Reaction

$$*\beta\text{-decay GT tra. rate} = \frac{1}{t_{1/2}} = \underbrace{f}_{\text{length}} \frac{\lambda^2}{K} \underbrace{B(\text{GT})}_{\text{structure}}$$

Study of Weak Response of Nuclei  
by means of  
Strong Interaction !  
using  $\beta$ -decay as a reference

$$\underbrace{\text{operator}}_{\text{structure}} = (\text{matrix element})^2$$

A simple reaction mechanism should be achieved !

→ we have to go to high incoming energy

**\*\*Connection between  
 $\beta$ -decay and ( $^3\text{He},t$ ) reaction\*\***

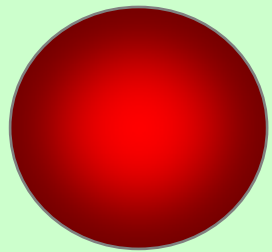
**by means of  
Isospin Symmetry**

T=1 Isospin Symmetry

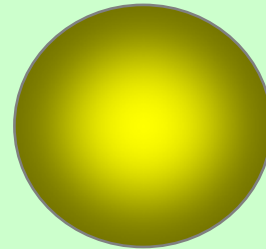


Byodoin-temple  
宇治・平等院

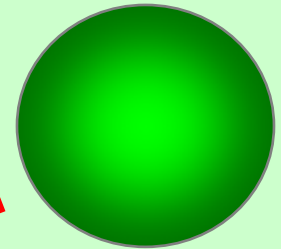
# T=1 Isospin Symmetry



GT



GT



$$T_z = +1$$



$$T_z = 0$$



$$T_z = -1$$

# Transitions in real & isospin space (T=1)

Symmetry Transitions from T=1 Nuclei

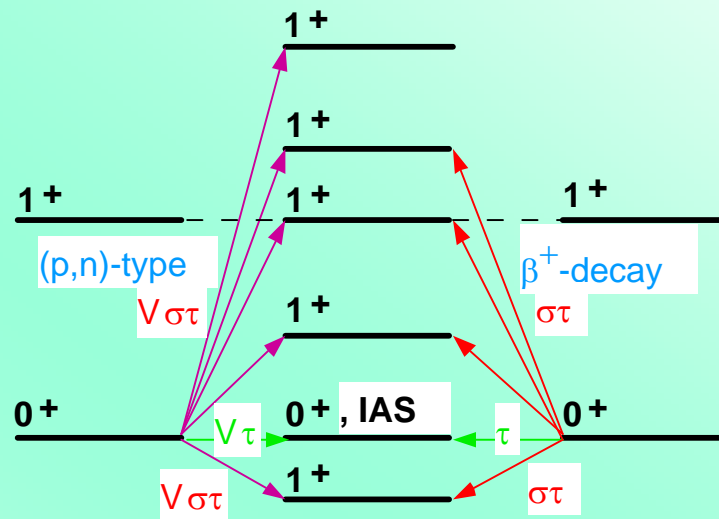
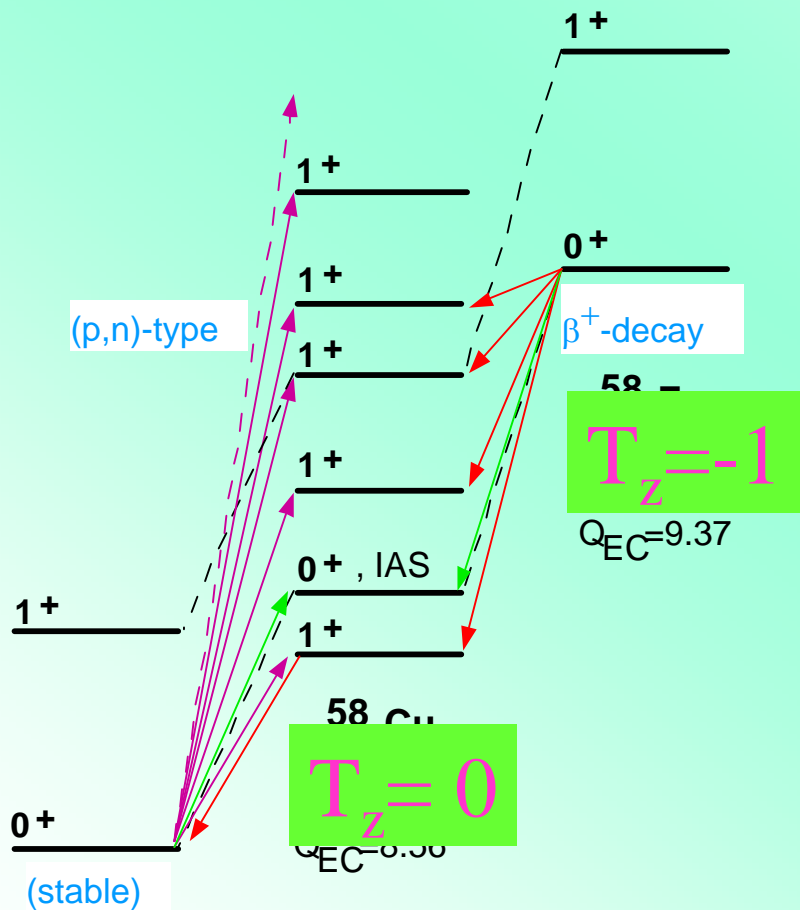
$$T_z=+1 \rightarrow T_z=0 \leftarrow T_z=-1$$

(in real energy space)

Symmetry Transitions from T=1 Nuclei

$$T_z=+1 \rightarrow T_z=0 \leftarrow T_z=-1$$

(in isospin symmetry space\*)



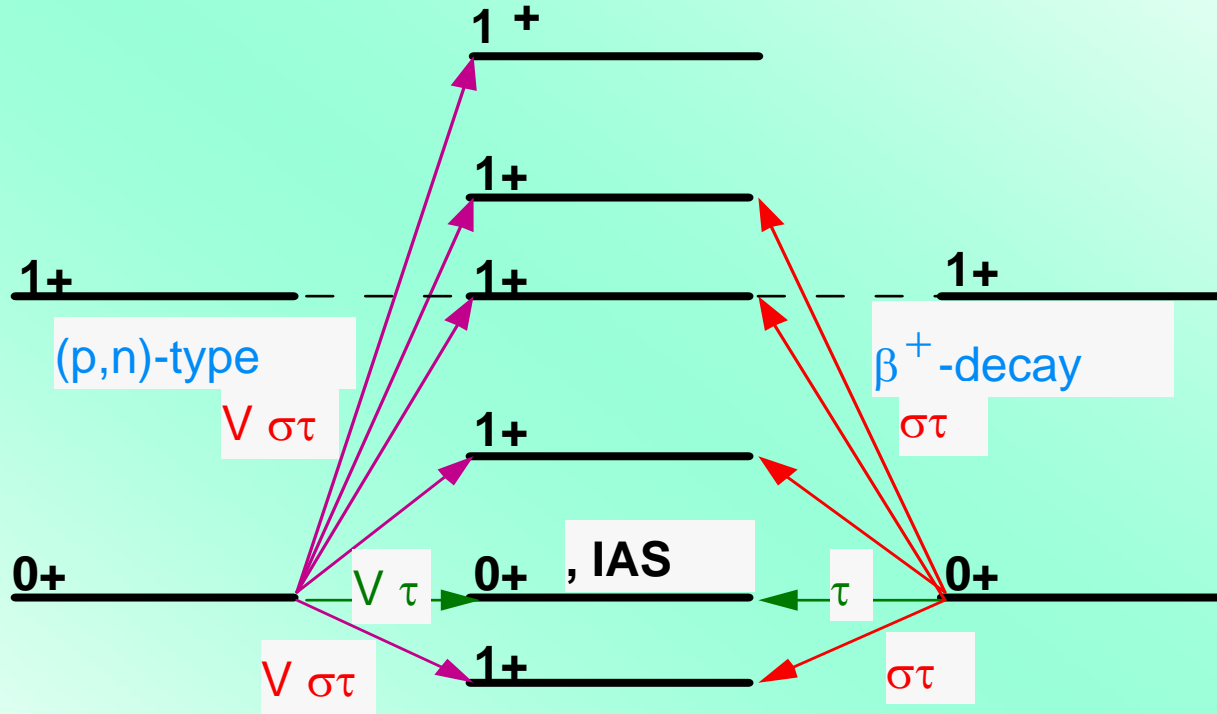
$T_z=+1$

\*after the correction of Coulomb displacement energy

# T=1 symmetry : Structures & Transitions

$$T_z=+1 \quad \longrightarrow \quad T_z=0 \quad \longleftarrow \quad T_z=-1$$

(in isospin symmetry space\*)



$T_z=+1$

$T_z=0$

$T_z=-1$

$^{26}\text{Mg}$

$^{26}\text{Al}$

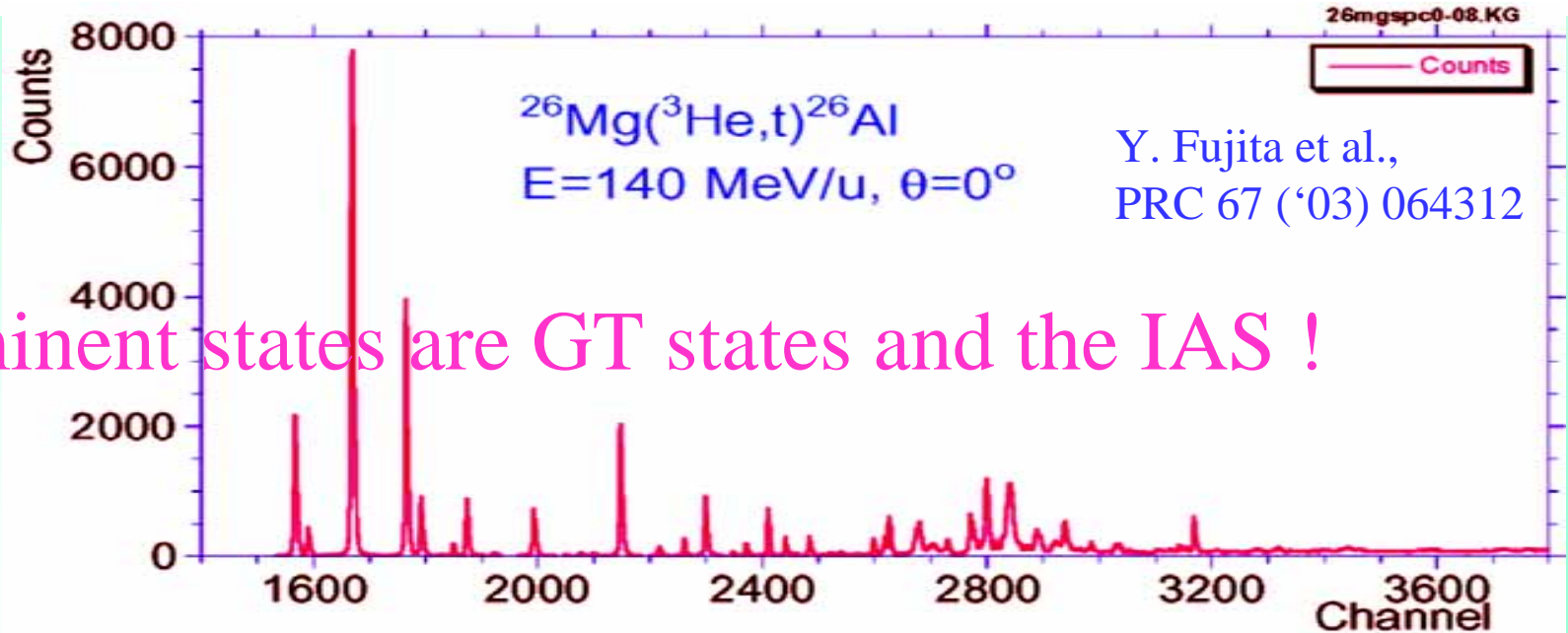
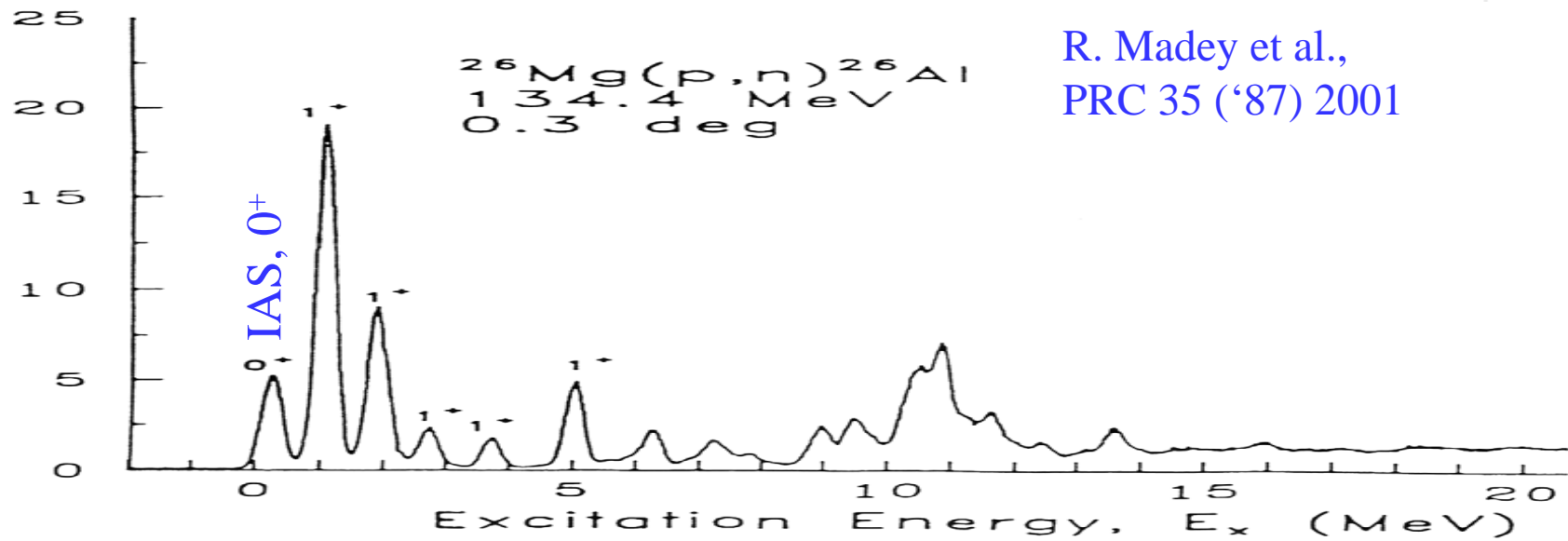
$^{26}\text{Si}$

Z=12, N=14

Z=13, N=13

Z=14, N=12

# $^{26}\text{Mg}(p, n)^{26}\text{Al}$ & $^{26}\text{Mg}(^3\text{He}, t)^{26}\text{Al}$ spectra



Prominent states are GT states and the IAS !



# B(GT) values from Symmetry Transitions (A=26)

$(^3\text{He}, t)$

B(GT)

0.106(4)

1+ ————— 3.724

0.117(4)

1+ ————— 2.740

0.113(5)

0.112(4)

1+ ————— 2.072

0.091(4)

0.527(15)

1+ ————— 1.851

0.537(14)

1.081(29)

1+ ————— 1.058

1.098(22)

0+

IAS

0+ ————— 0.228

0+

5+

$^{26}\text{Mg}$

$^{26}\text{Al}$

$^{26}\text{Si}$

$T_z=+1$

$T_z=0$

$T_z=-1$

$\beta$ -decay

B(GT)

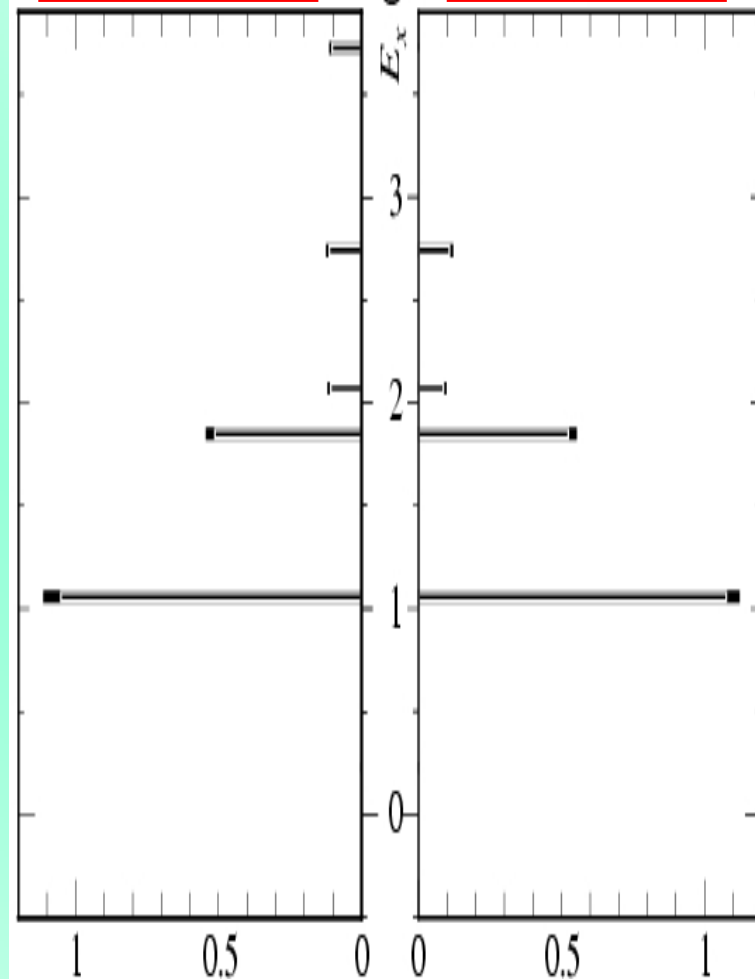
Experiments

$^{26}\text{Mg} \rightarrow ^{26}\text{Al}$

$^{26}\text{Si} \rightarrow ^{26}\text{Al}$

$^{26}\text{Mg} (^3\text{He}, t) ^{27}\text{Al}$

$\beta_+$  decay



# B(GT) values from Symmetry Transitions

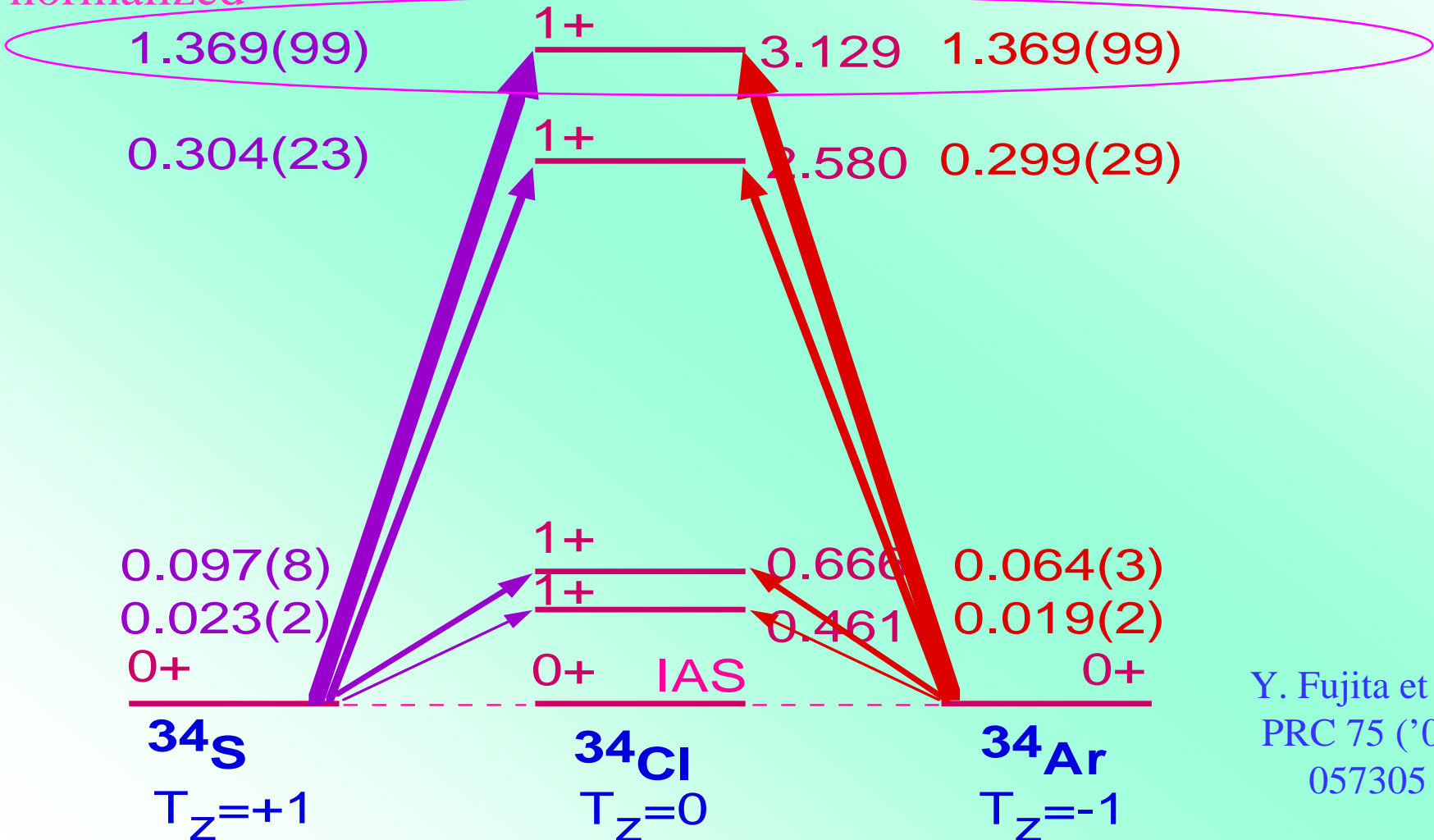
(A=34) from  $\beta$ -decay

from ( $^3\text{He},t$ )

B(GT)

B(GT)

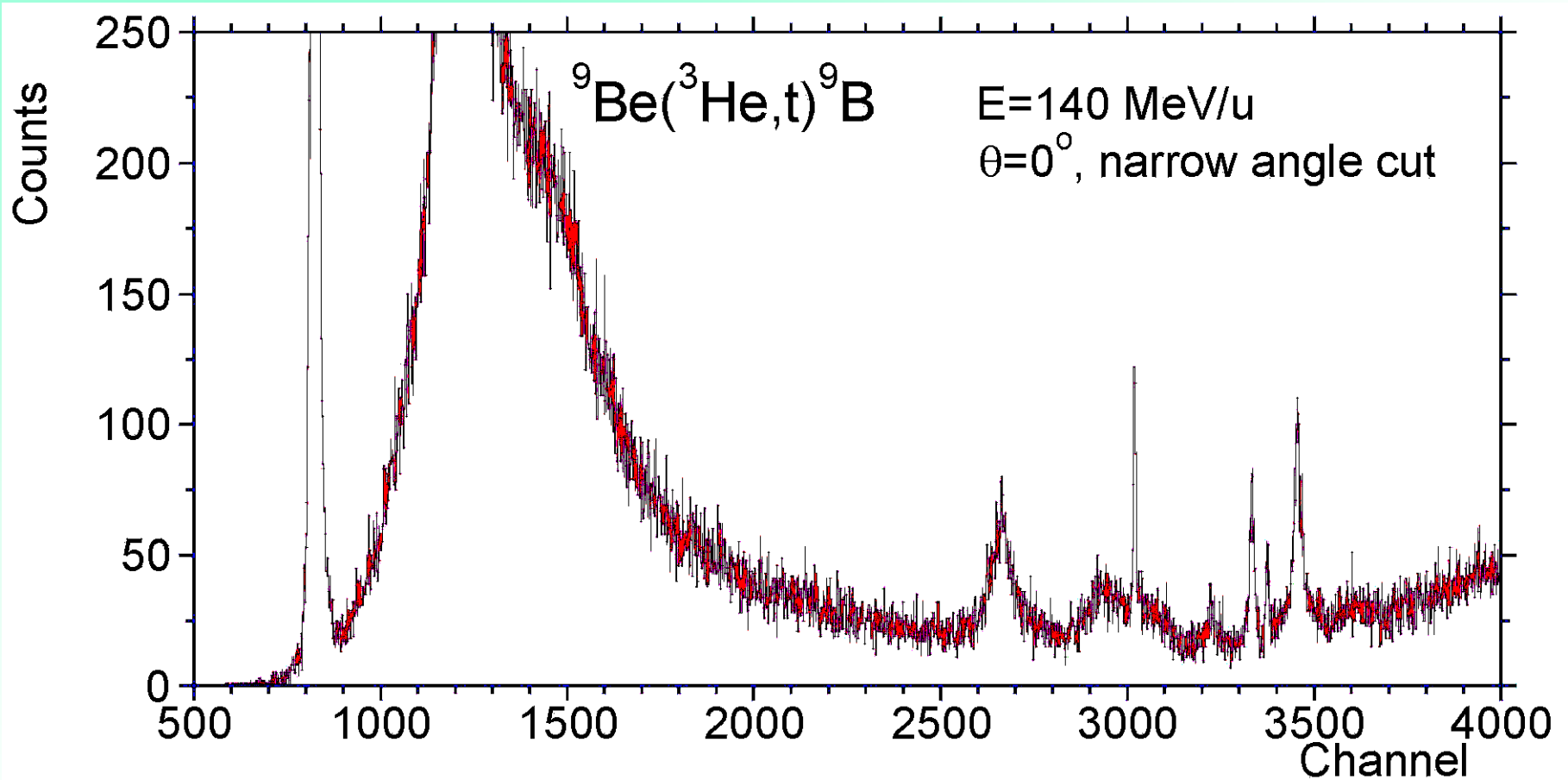
normalized



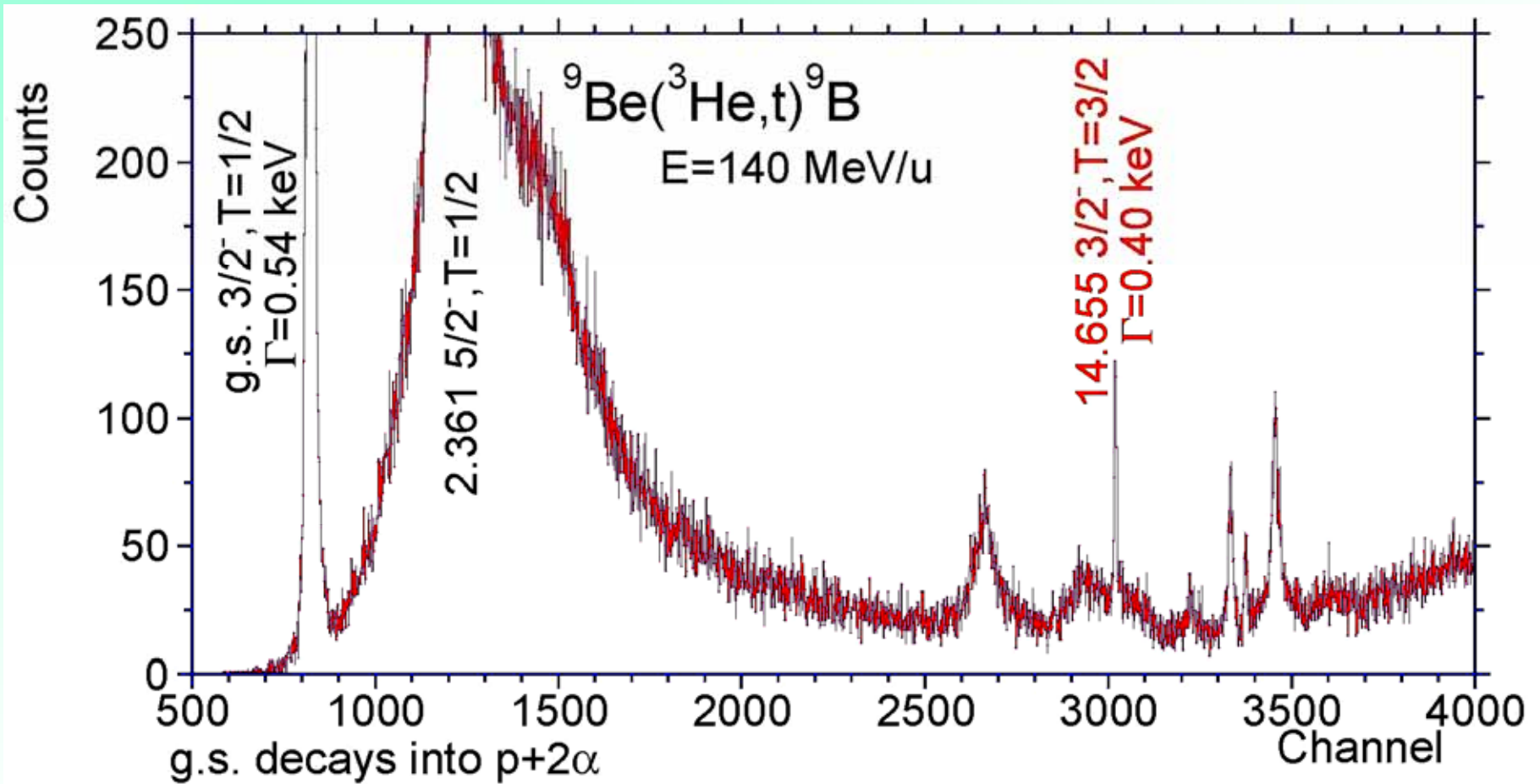
Y. Fujita et al.,  
 PRC 75 ('07)  
 057305

**\*\*(<sup>3</sup>He, t): high resolution and sensitivity !**

# ${}^9\text{Be}({}^3\text{He},t){}^9\text{B}$ spectrum (at various scales)



# ${}^9\text{Be}({}^3\text{He}, t){}^9\text{B}$ spectrum (II)



**Isospin selection rule prohibits  
proton decay of  $T=3/2$  state!**

C. Scholl, Koeln

# Relationship: Decay and Width

Heisenberg's Uncertainty Principle

$$\Delta x \cdot \Delta p \approx \hbar$$

$$\Delta t \cdot \Delta E \approx \hbar$$

Width  $\Gamma = \Delta E$

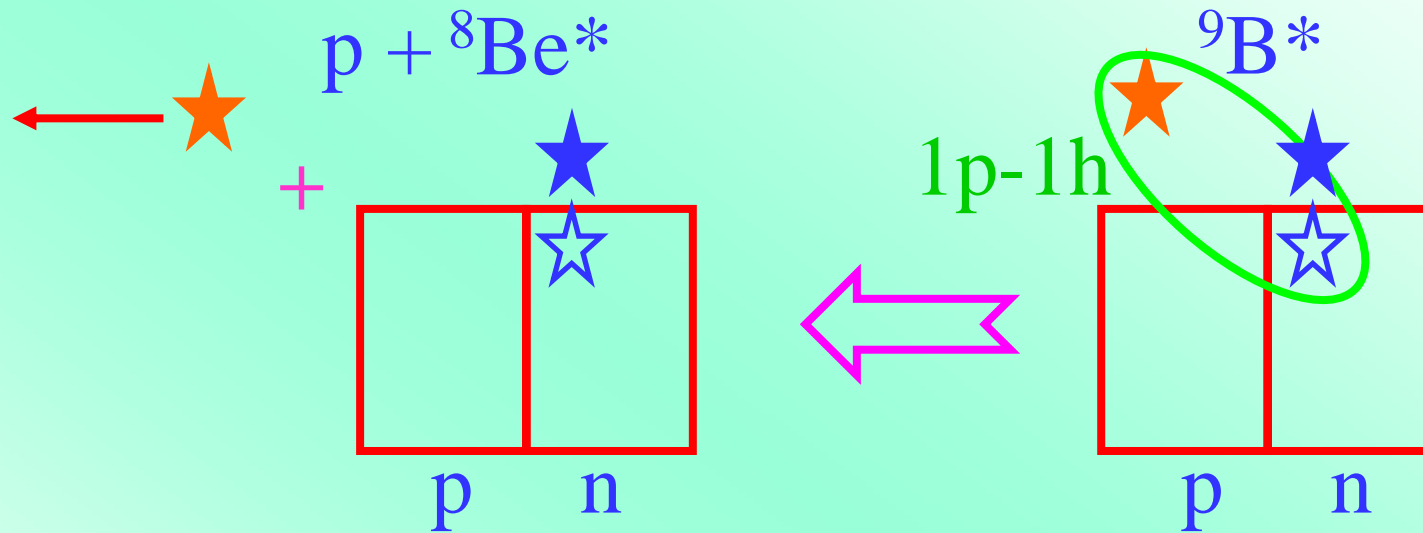
\*if: Decay is Fast,

then: Width of a State is Wider !

\*if  $\Delta t = 10^{-20}$  sec  $\rightarrow \Delta E \sim 100$  keV (particle decay)

$\Delta t = 10^{-15}$  sec  $\rightarrow \Delta E \sim 1$  eV (fast  $\gamma$  decay)

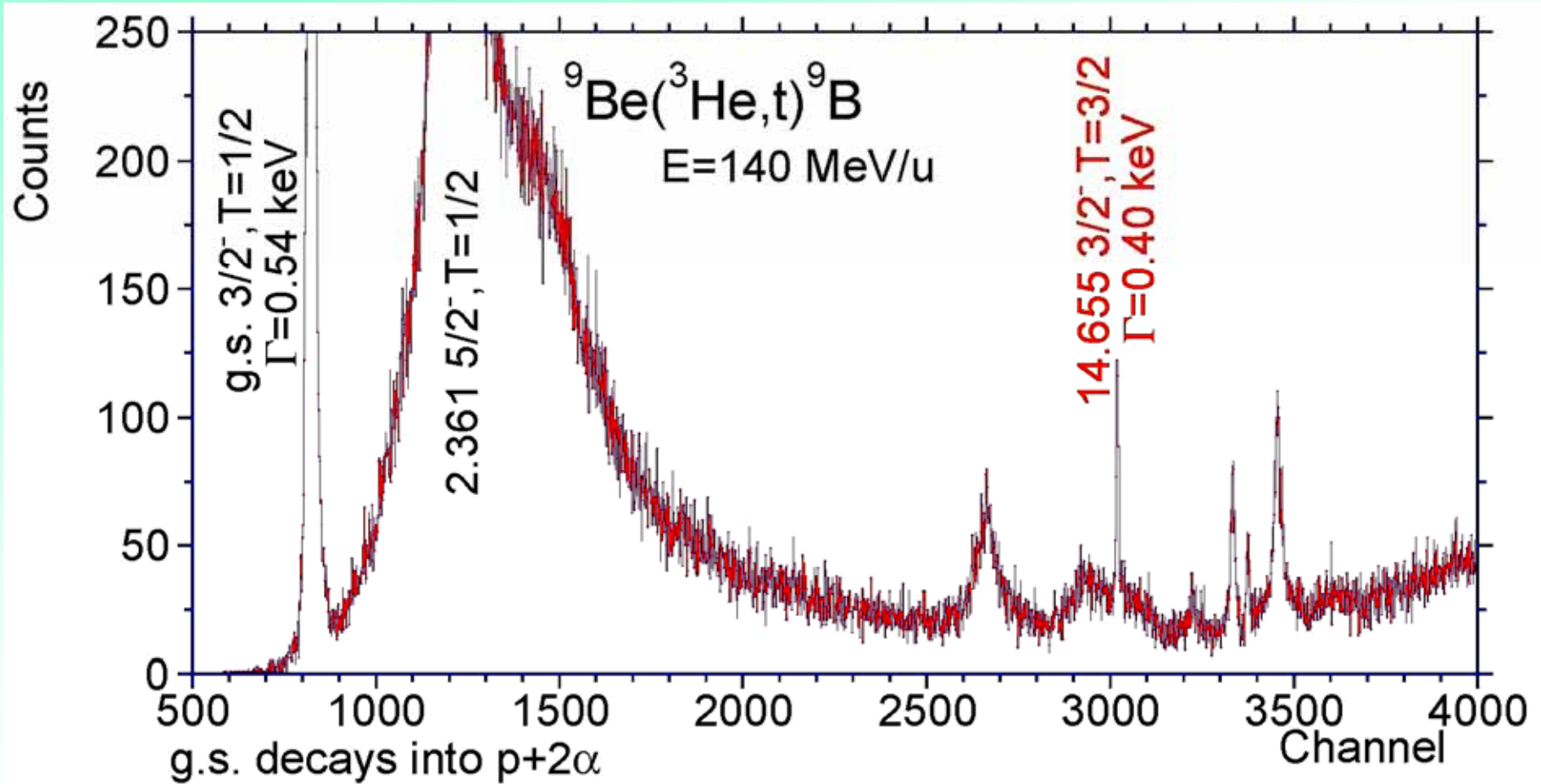
# Isospin Selection Rule : in $p$ -decay of ${}^9\text{B}$



$$\begin{array}{l}
 T_z : -1/2 + 0 = -1/2 \\
 T : 1/2 + 0 \text{ (low lying)} = 1/2 \\
 T : 1/2 + 1 \text{ (higher Ex)} = 1/2 \ \& \ 3/2
 \end{array}$$

\*T=1 state in  ${}^8\text{Be}$  is only above  $E_x=16.6 \text{ MeV}$

# ${}^9\text{Be}({}^3\text{He}, t){}^9\text{B}$ spectrum (III)



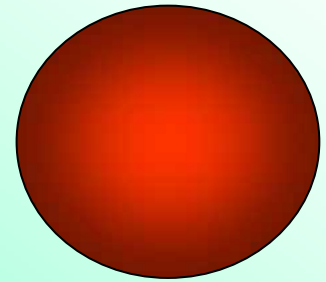
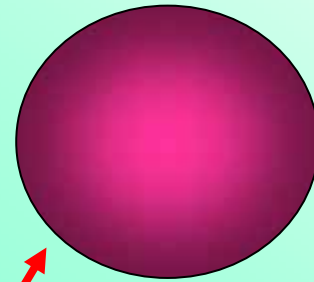
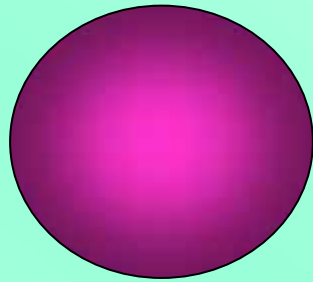
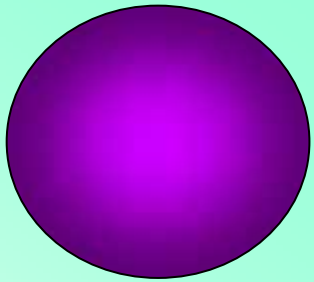
**14.7 MeV  $T=3/2^-$  state is very weak!**

Strength ratio of g.s. & 14.7 MeV  $3/2^-$  states: **140:1**



# Shell Structure and Cluster Structure

$T=3/2$  Excited state: SM-like



${}^9\text{Li}$

$T_z=3/2$

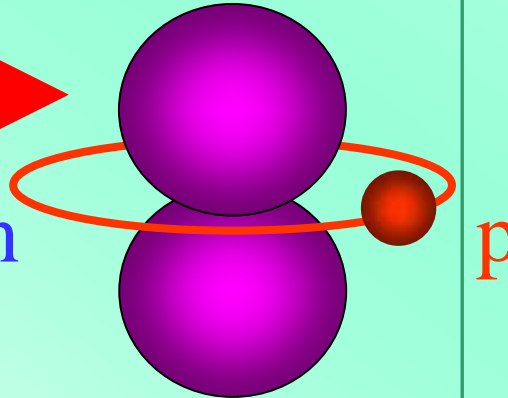
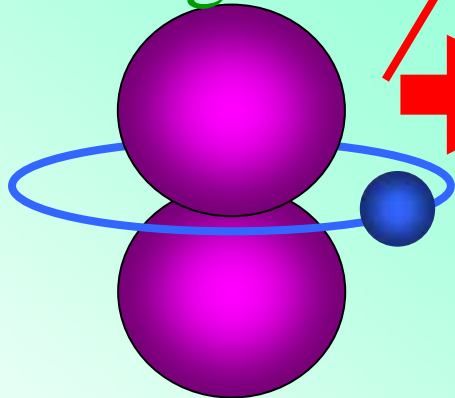
neutron:  $p_{3/2}$  closed

${}^9\text{C}$

$T_z=-3/2$

proton:  $p_{3/2}$  closed

g.s.: Cluster-like



${}^9\text{Be}$

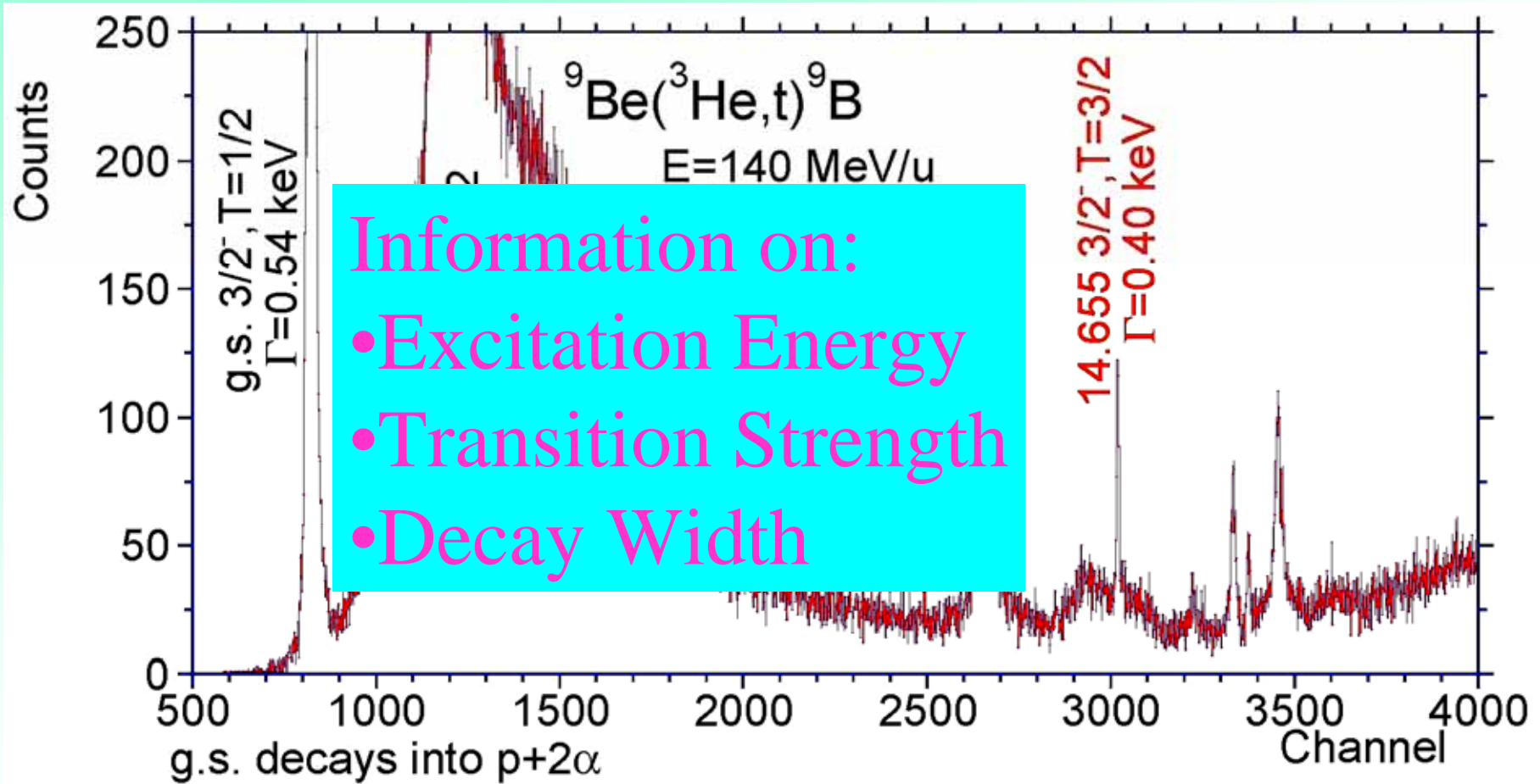
$T_z=1/2$

${}^9\text{B}$

$T_z=-1/2$

suggestion by  
Y. Kanada-En'yo

# ${}^9\text{Be}({}^3\text{He}, t){}^9\text{B}$ spectrum (III)



**14.7 MeV  $T=3/2^-$  state is very weak!**

Strength ratio of g.s. & 14.7 MeV  $3/2^-$  states: **140:1**

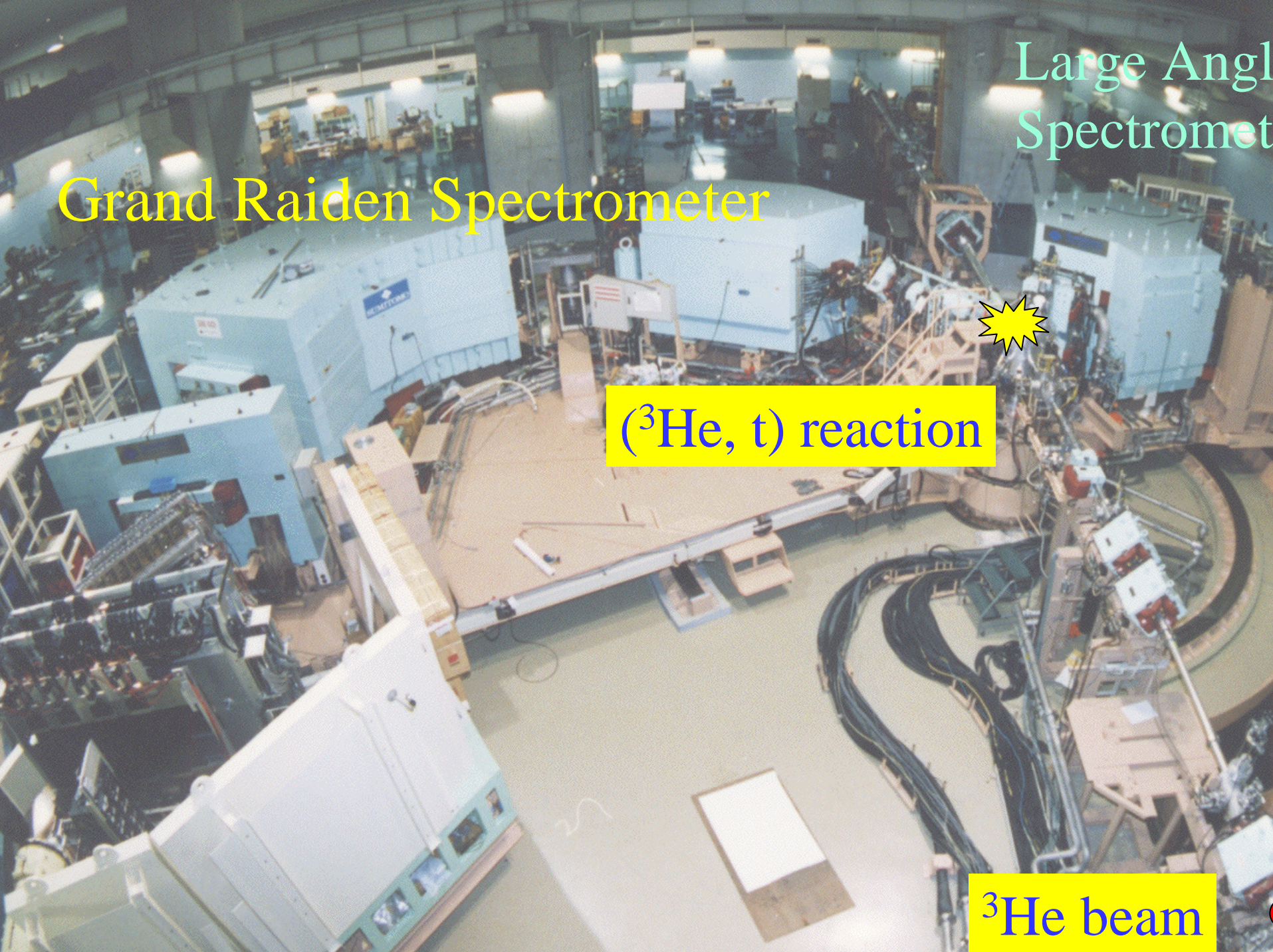
# High-resolution Experiment

-beam matching techniques-  
(dispersion matching techniques)

# RCNP Ring Cyclotron

Good quality  $^3\text{He}$  beam (140 MeV/nucleon)





Large Angle  
Spectrometer

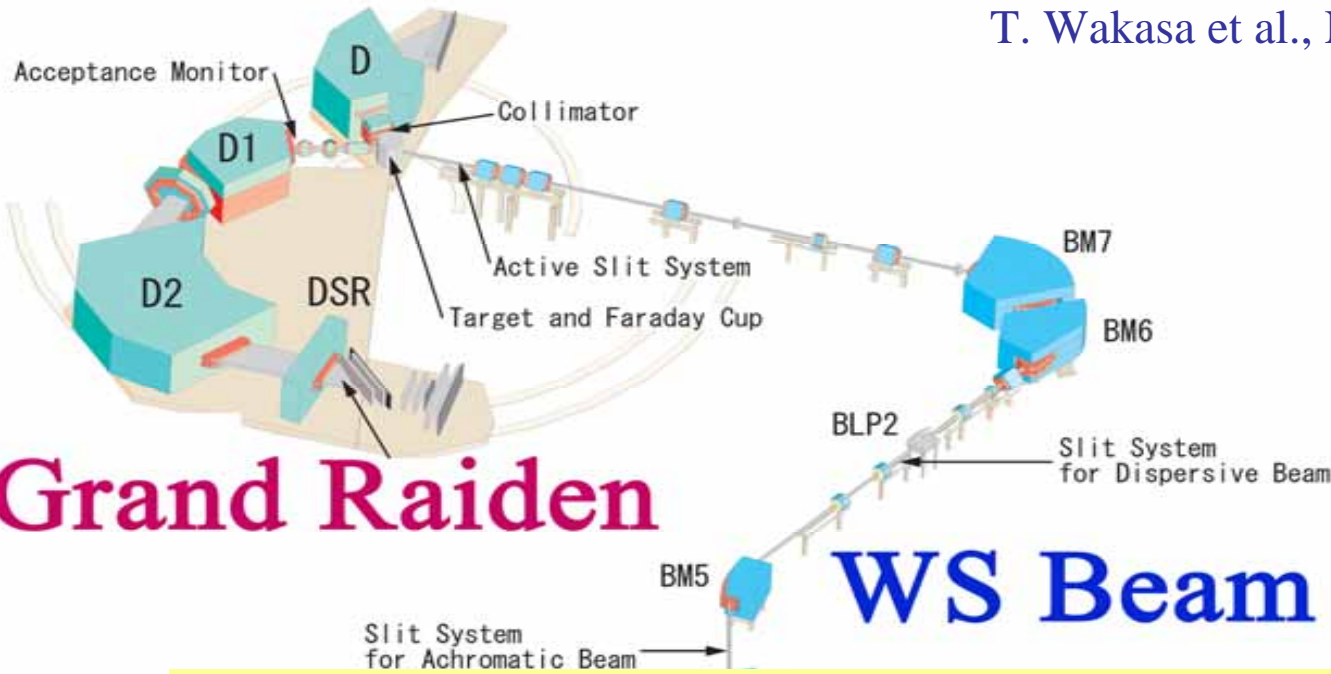
Grand Raiden Spectrometer

$(^3\text{He}, t)$  reaction

$^3\text{He}$  beam

# Beam line WS-course at RCNP

T. Wakasa et al., NIM A482 ('02) 79.



**Grand Raiden**

**WS Beam Line**

**Dispersion Matching Techniques**

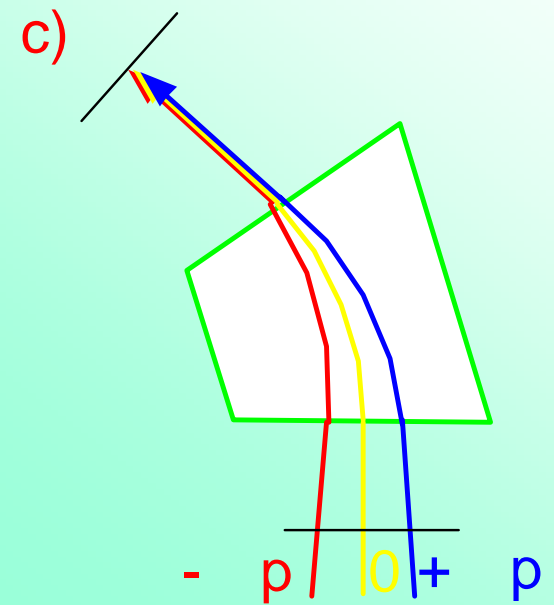
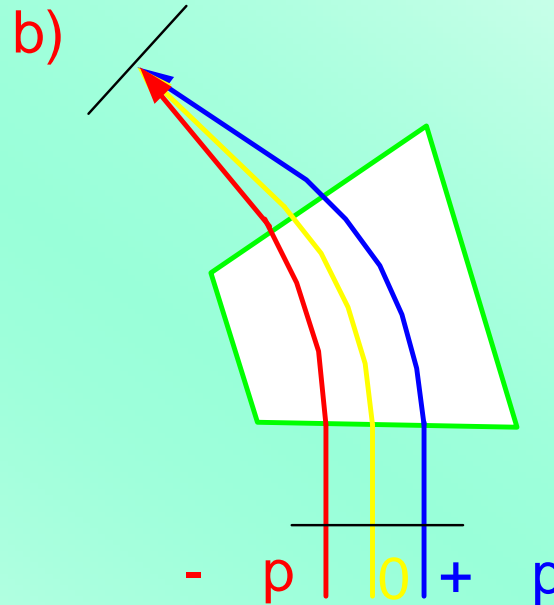
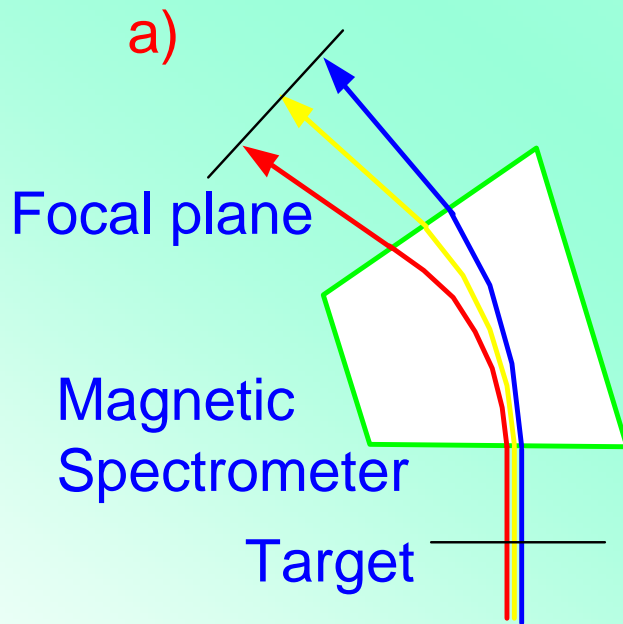
**Ring Cyclotron**



# Matching Techniques

Y. Fujita et al., N.I.M. B 126 (1997) 274.

H. Fujita et al., N.I.M. A 484 (2002) 17.



*Achromatic beam transportation*

$\Delta E \sim 200 \text{ keV}$   
for  $140 \text{ MeV/u } ^3\text{He}$  beam

*Lateral dispersion matching*

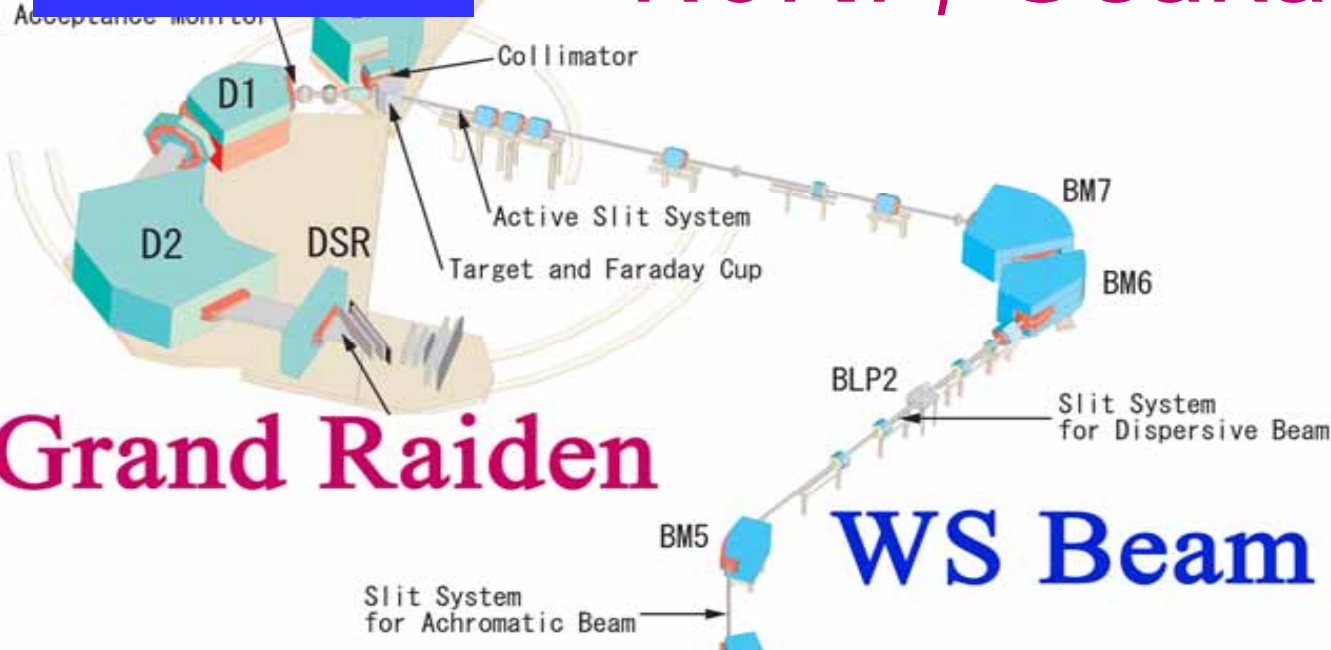
$\Delta E \sim 35 \text{ keV}$   
Horiz. angle resolution  
 $\Delta\theta_{\text{sc}} > 15 \text{ mrad}$

*Angular dispersion matching*

$\Delta\theta_{\text{sc}} \sim 5 \text{ mrad}$

$\Delta E=30 \text{ keV}$

RCNP, Osaka Univ.



Grand Raiden

WS Beam Line

Dispersion Matching Techniques  
were applied!

$\Delta E=150 \text{ keV}$

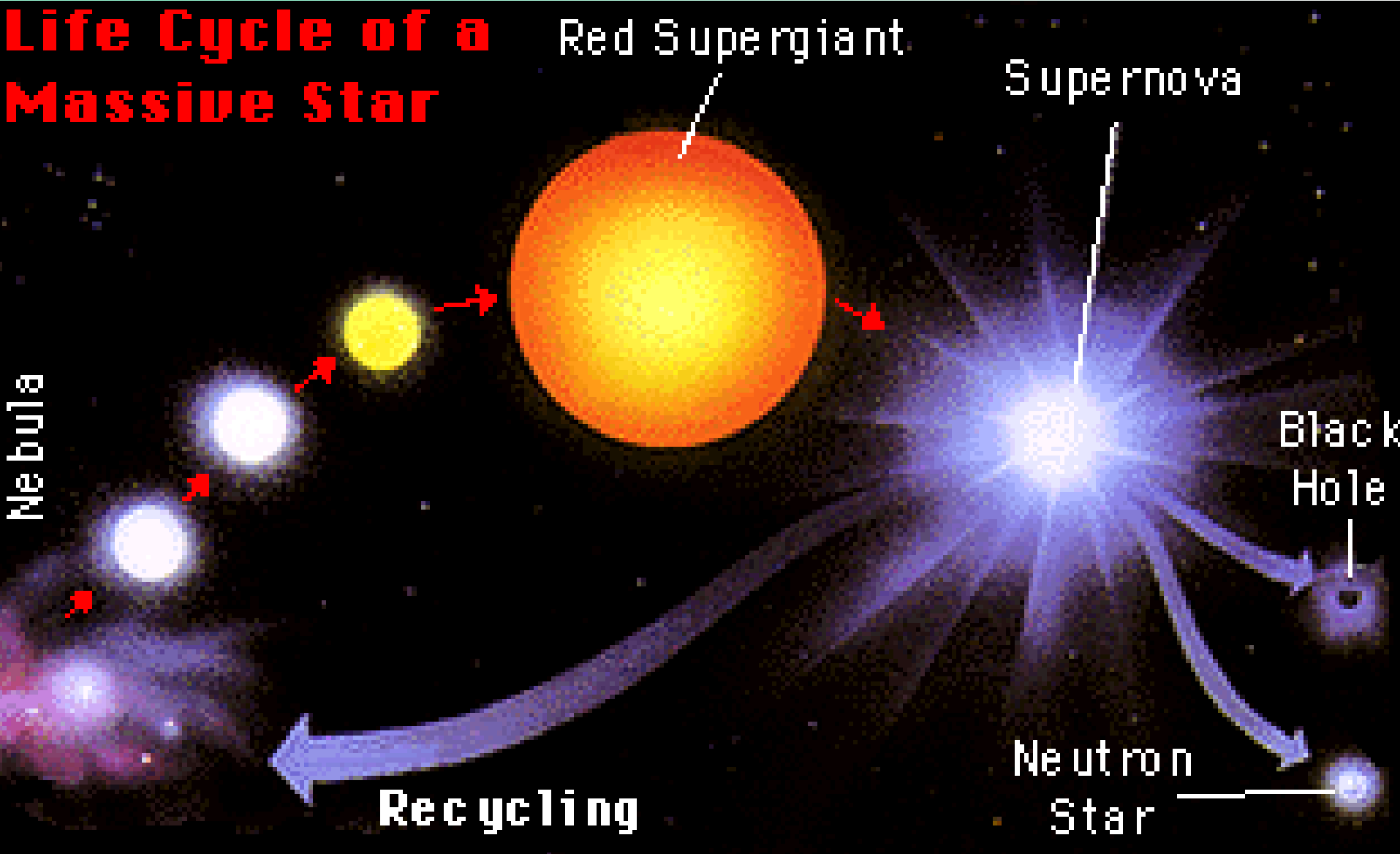
Ring Cyclotron





# Supernova Cycle

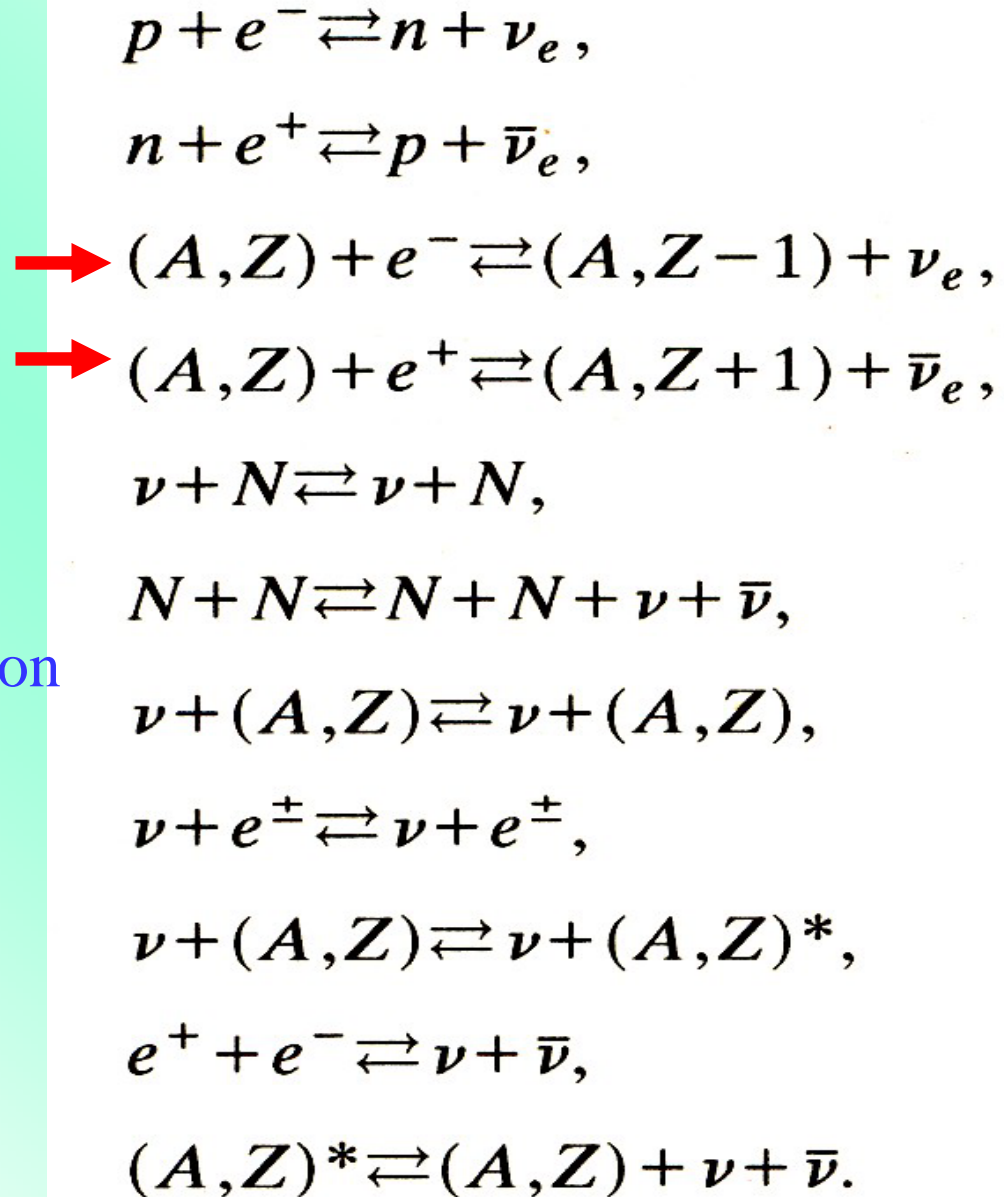
## Life Cycle of a Massive Star



# Crucial Weak Processes during the Core Collapse

$\sigma\tau$ : important

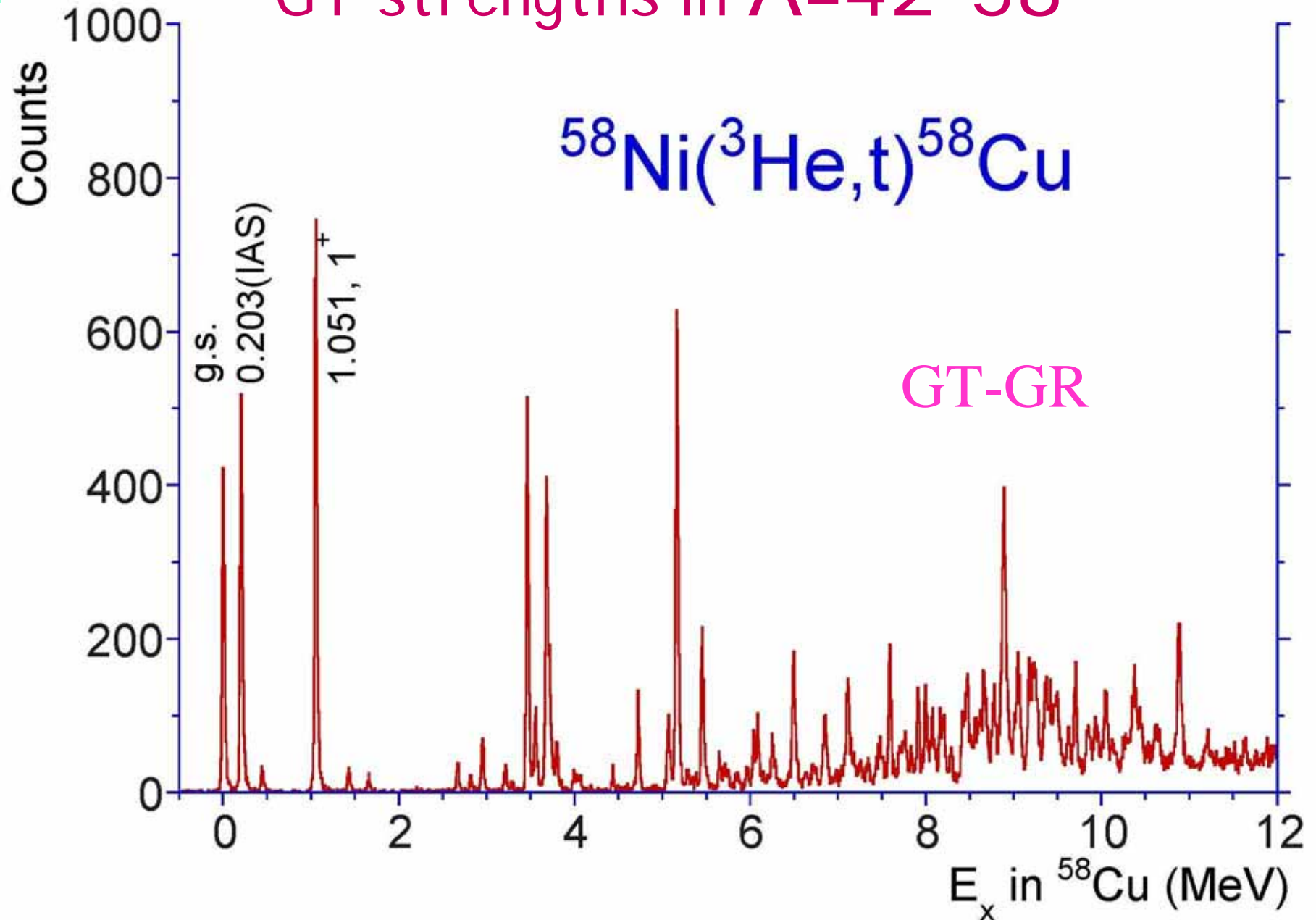
$(A, Z)$ =nuclei in the Cr, Mn, Fe, Co, Ni region  
*pf*-shell Nuclei !



Langanke & Martinez-Pinedo  
Rev.Mod.Phys.75('04)819

Balantekin & Fuller  
J.Phys.G 29('03)2513

# GT strengths in $A=42-58$



## \*\* Derivation of "absolute" B(GT) values

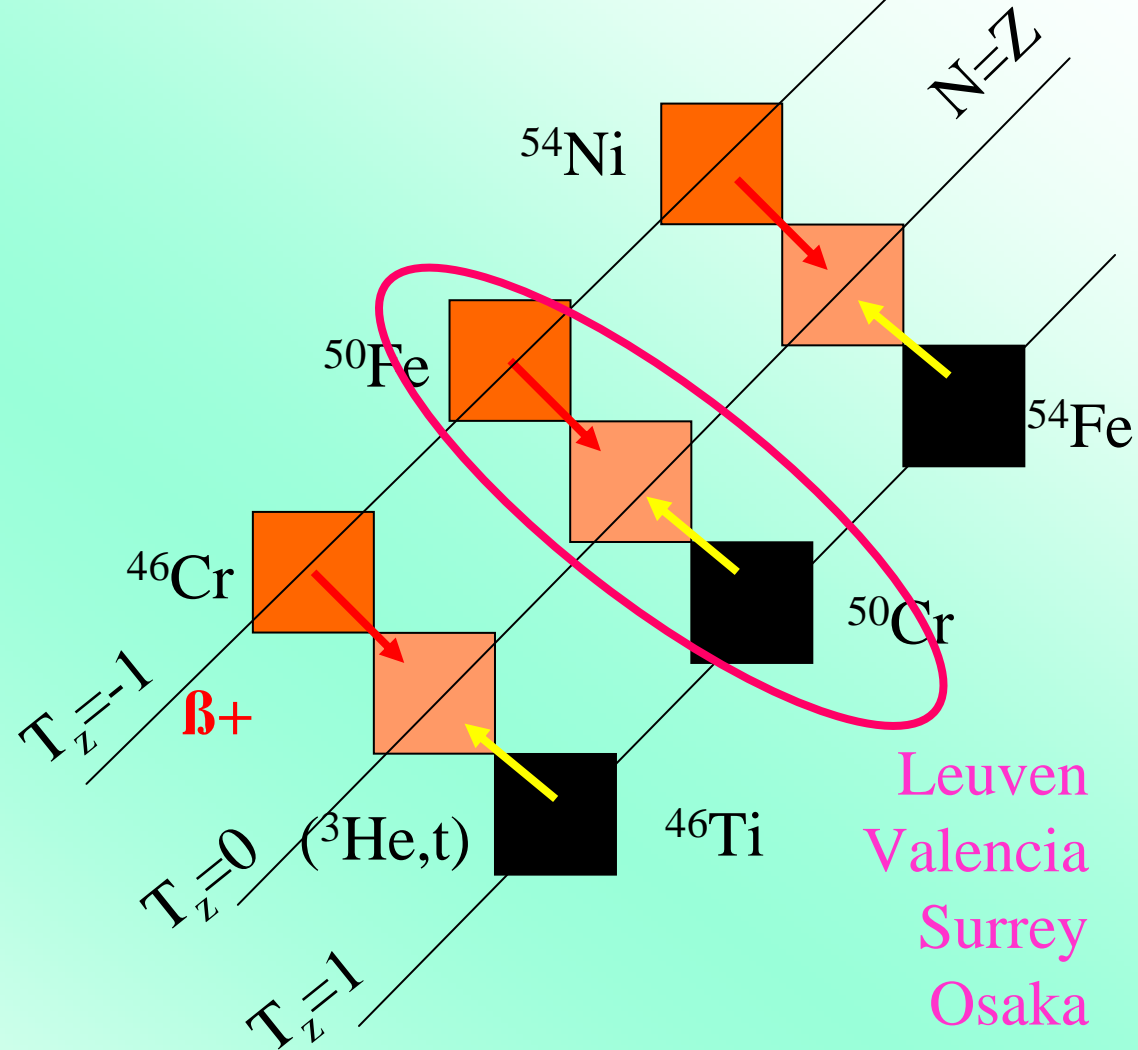
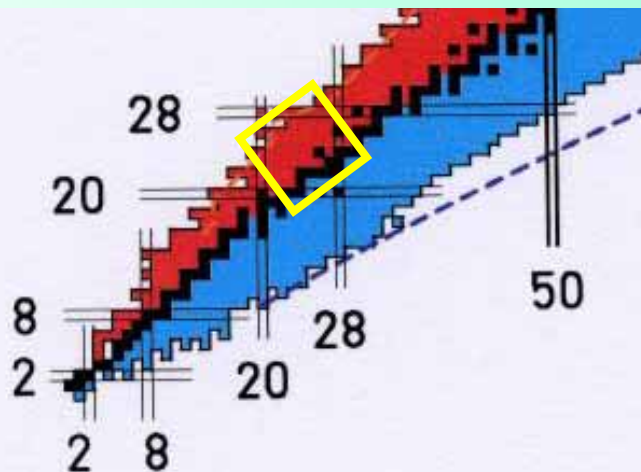
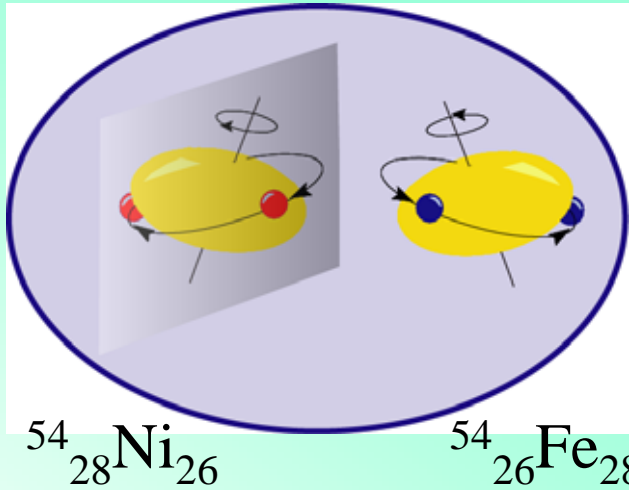
\*  $\beta$ -decay:  $T_{1/2}$  and absolute B(GT) values  
but only for the low-lying states

\* ( $^3\text{He}, t$ ) reaction: highly-excited states can be  
accessed but only the relative B(GT) values

Let's combine these data !

# T=1 Isospin Symmetry in *pf*-shell Nuclei

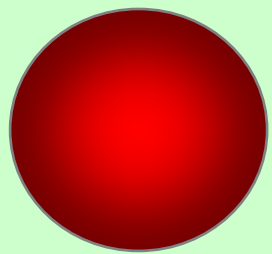
## Mirror nuclei



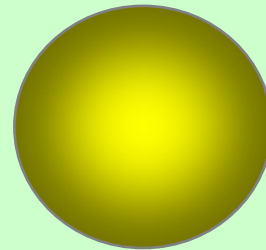
Leuven  
Valencia  
Surrey  
Osaka  
GSI

by B. Rubio

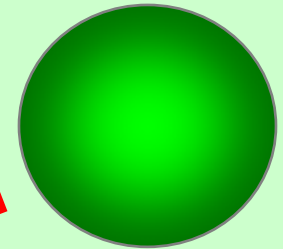
# T=1 Isospin Symmetry



GT



GT



$$T_z = +1$$

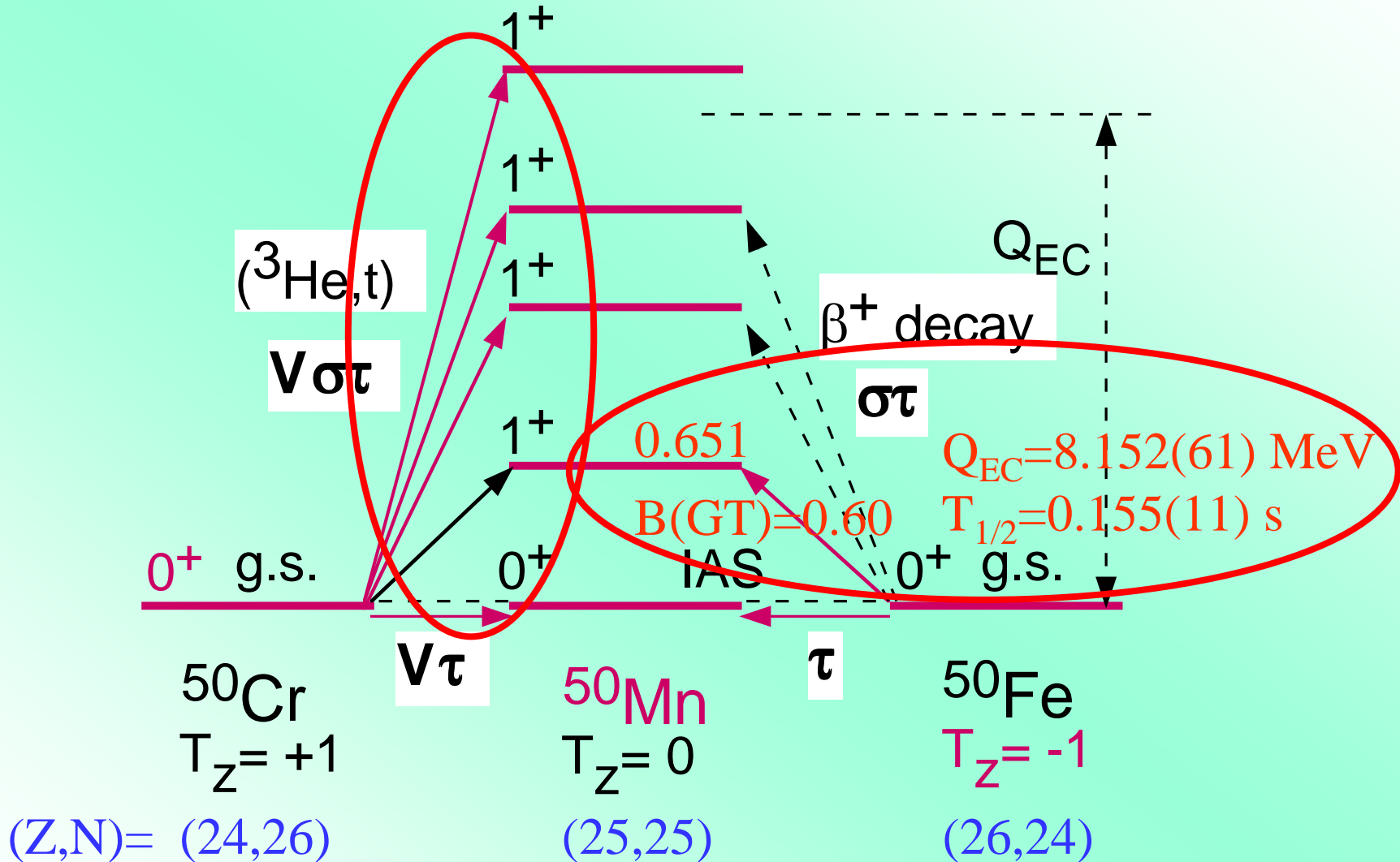


$$T_z = 0$$



$$T_z = -1$$

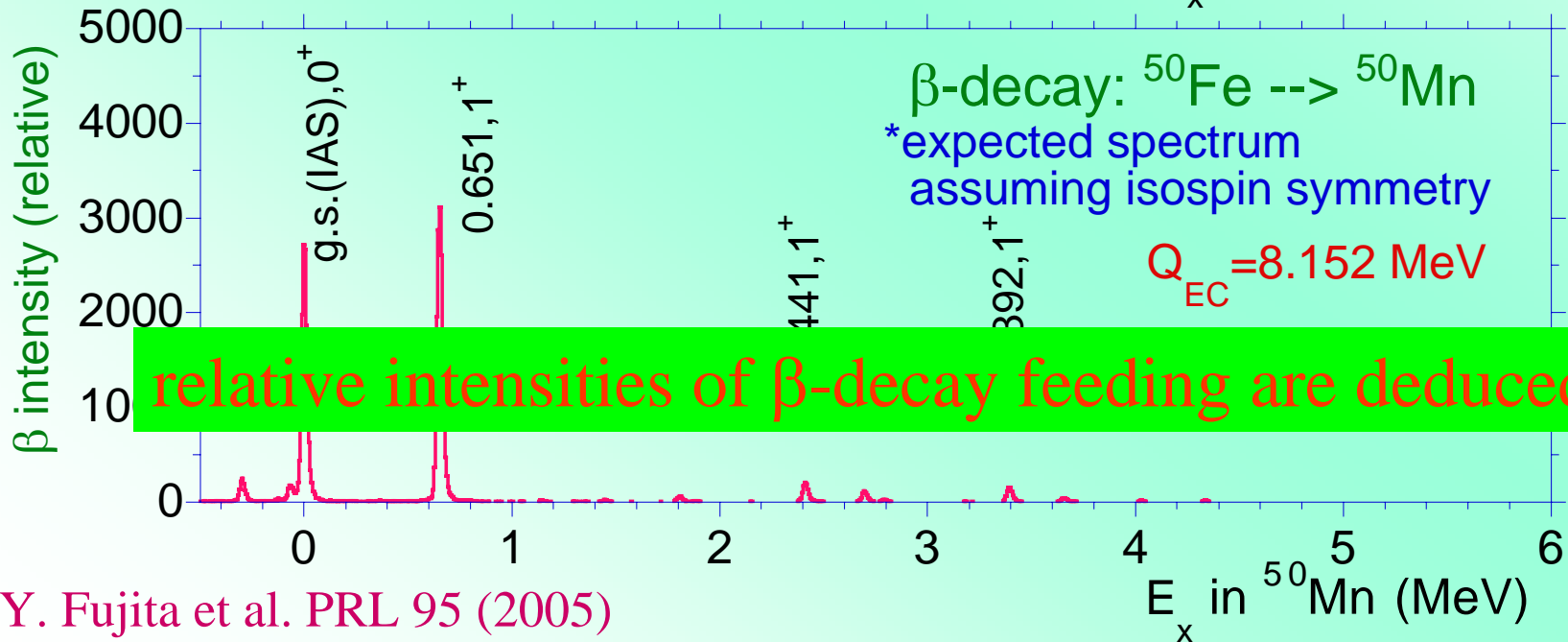
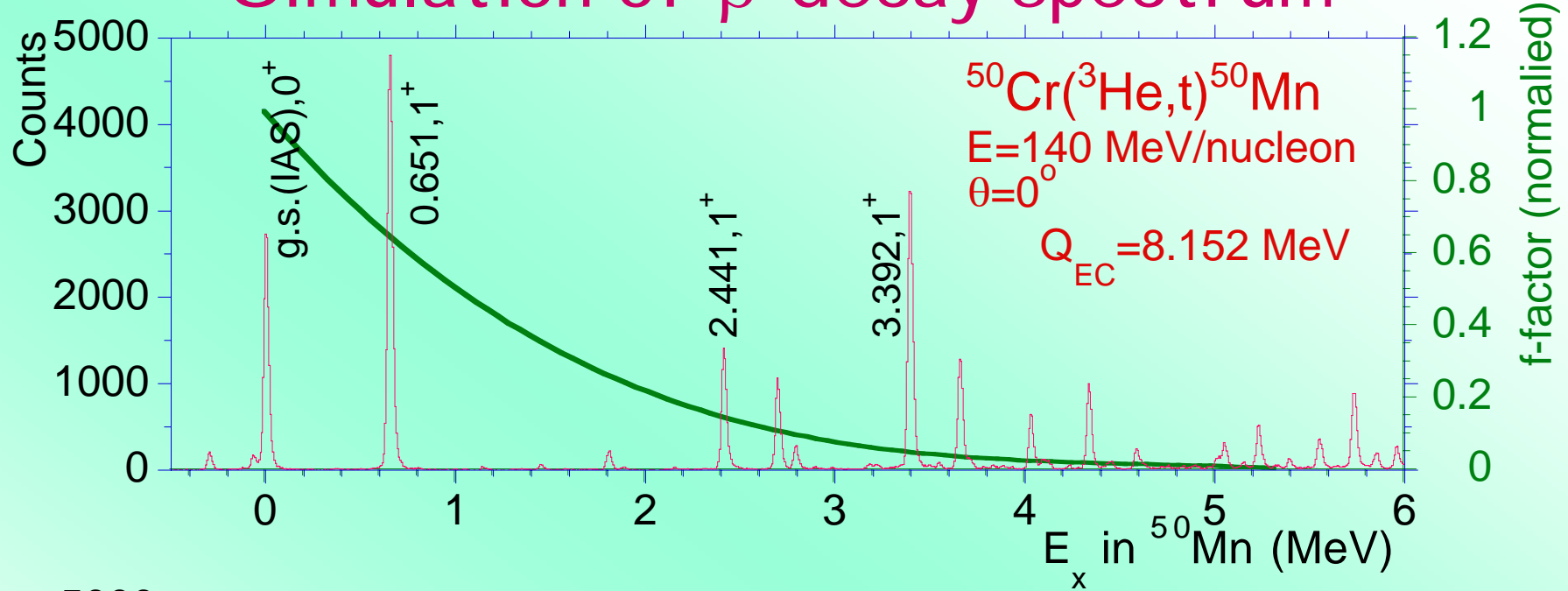
# Isospin Symmetry Transitions:



\*\*Reconstruction of  $\beta$  decay from ( ${}^3\text{He}, t$ )  
---assuming isospin symmetry ---



# Simulation of $\beta$ -decay spectrum



# Absolute B(GT) values

-via reconstruction of  $\beta$ -decay spectrum-

Tra.Strength  $\propto 1/t_i$   $t_i$  = partial half-life

$$\frac{1}{T_{1/2}} = \frac{1}{t_{Fermi}} + \sum_{i=GT} \frac{1}{t_i}$$

$\beta$ -decay  
experiment

$$T_{1/2} = 0.155(11) \text{ s}$$

$B(F) = N - Z$

Relative feeding intensity  
from ( $^3\text{He}, t$ )

Absolute intensity: B(GT)

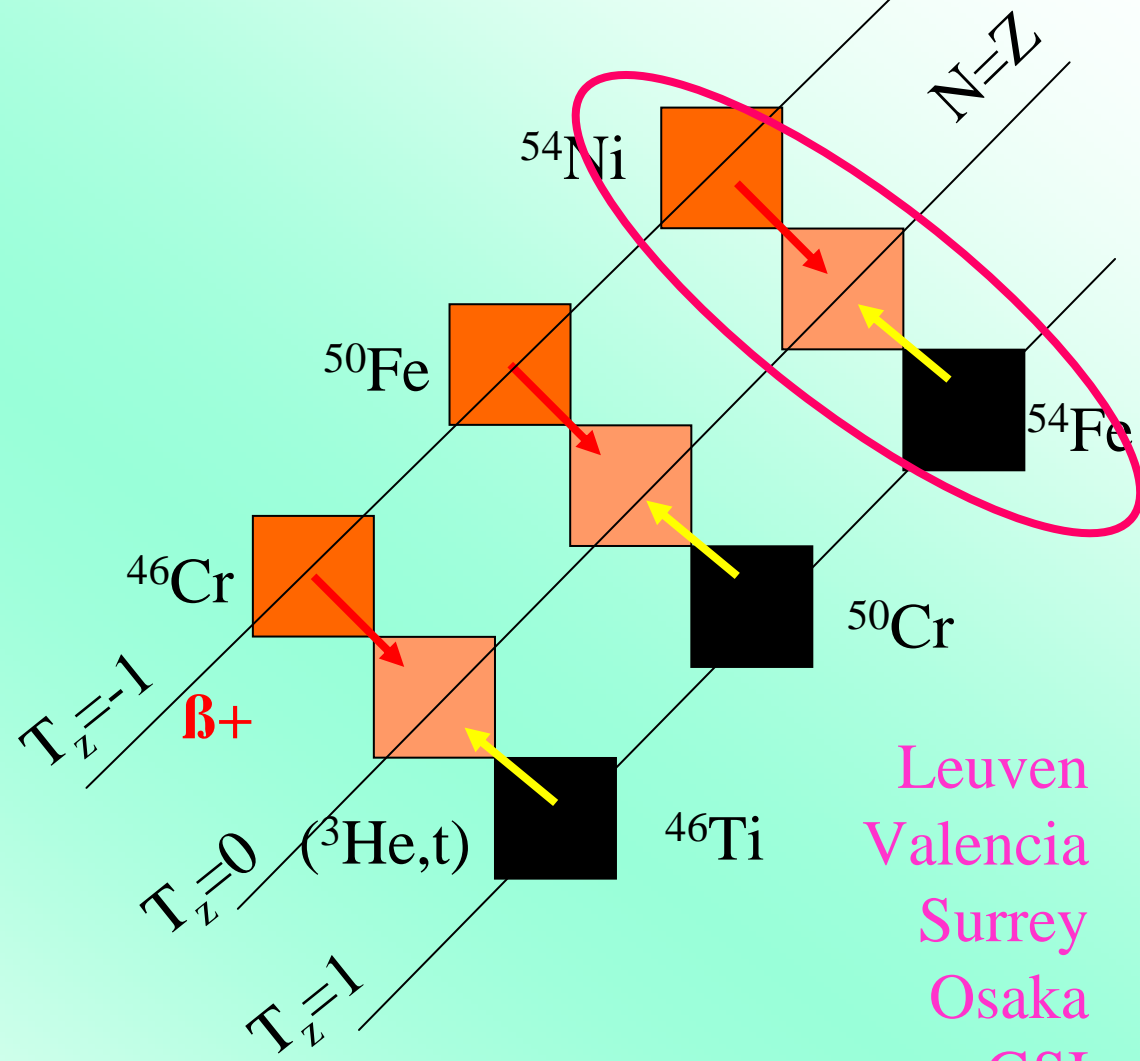
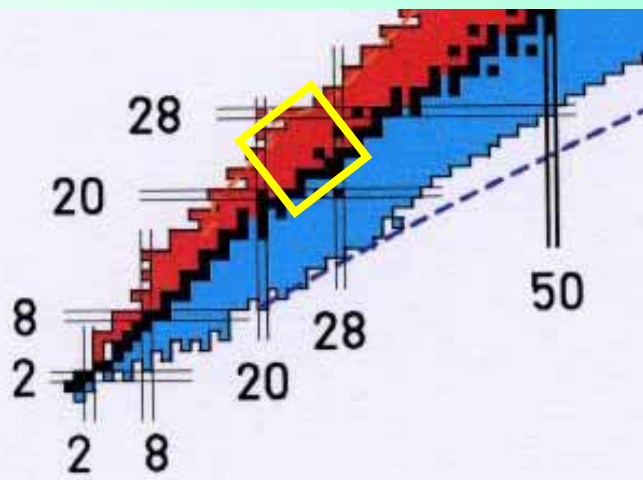
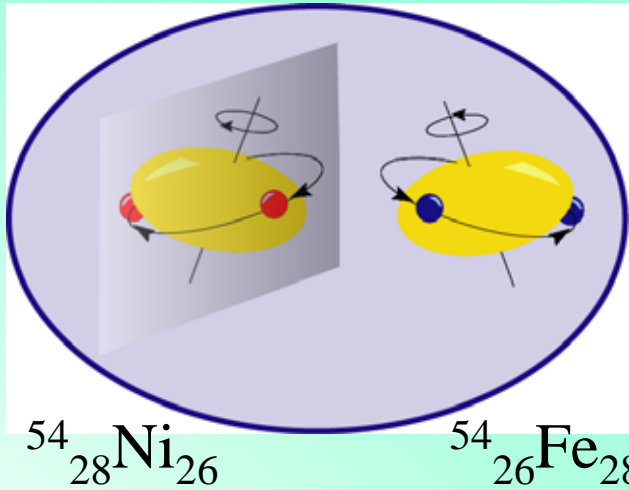
GT tra. to the 0.65 MeV state

New value B(GT) = 0.50(13)

\*20% smaller than deduced in the  $\beta$ -decay: 0.60(16)

# T=1 Isospin Symmetry in *pf*-shell Nuclei

## Mirror nuclei



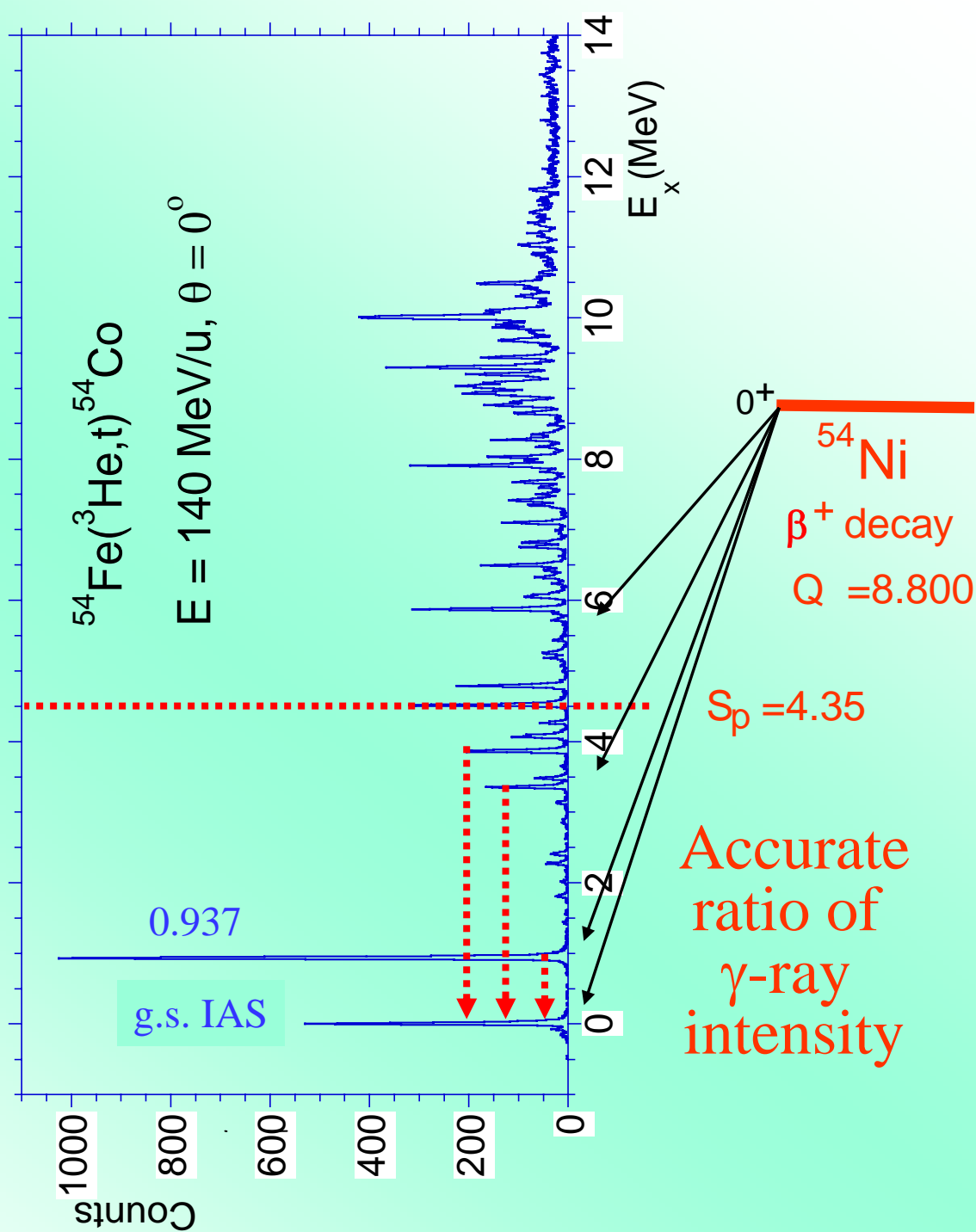
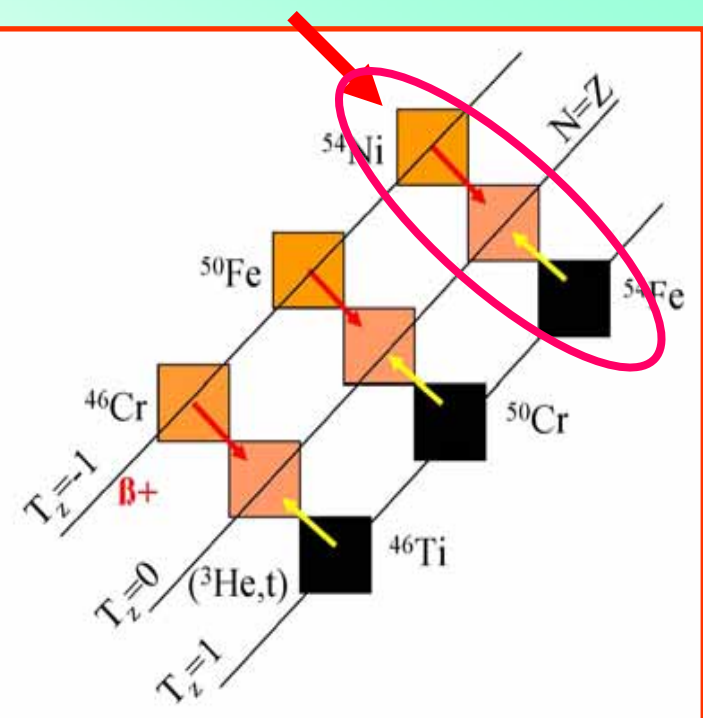
Leuven  
Valencia  
Surrey  
Osaka  
GSI  
CNS

by B. Rubio

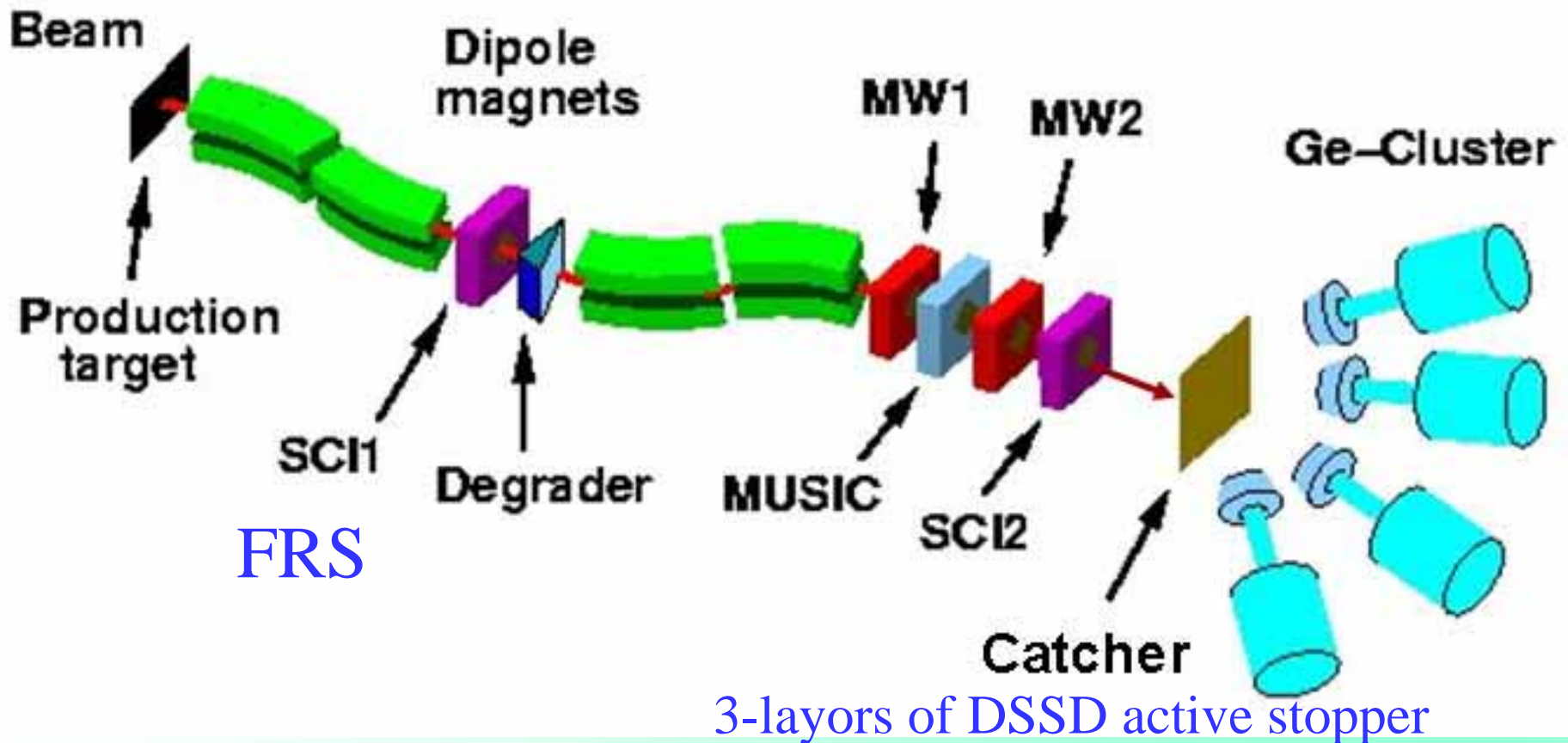
# $^{54}\text{Ni}$ $\beta$ -decay measurement

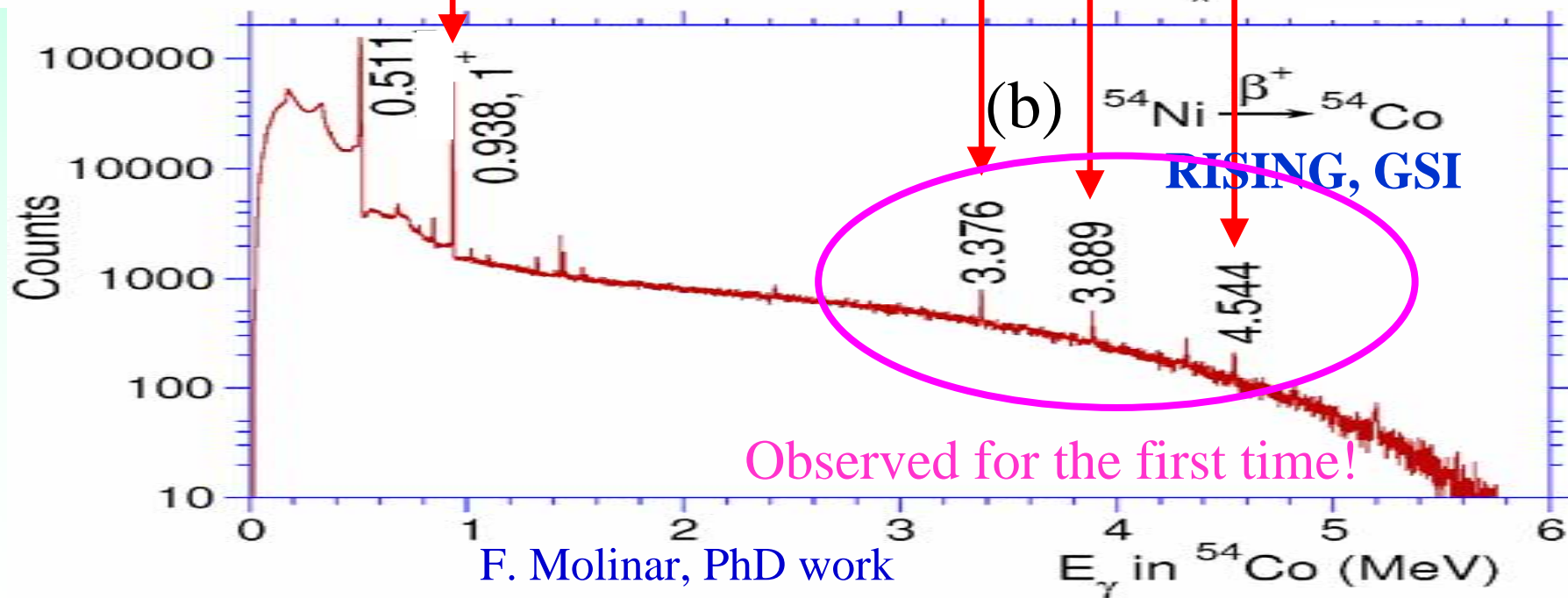
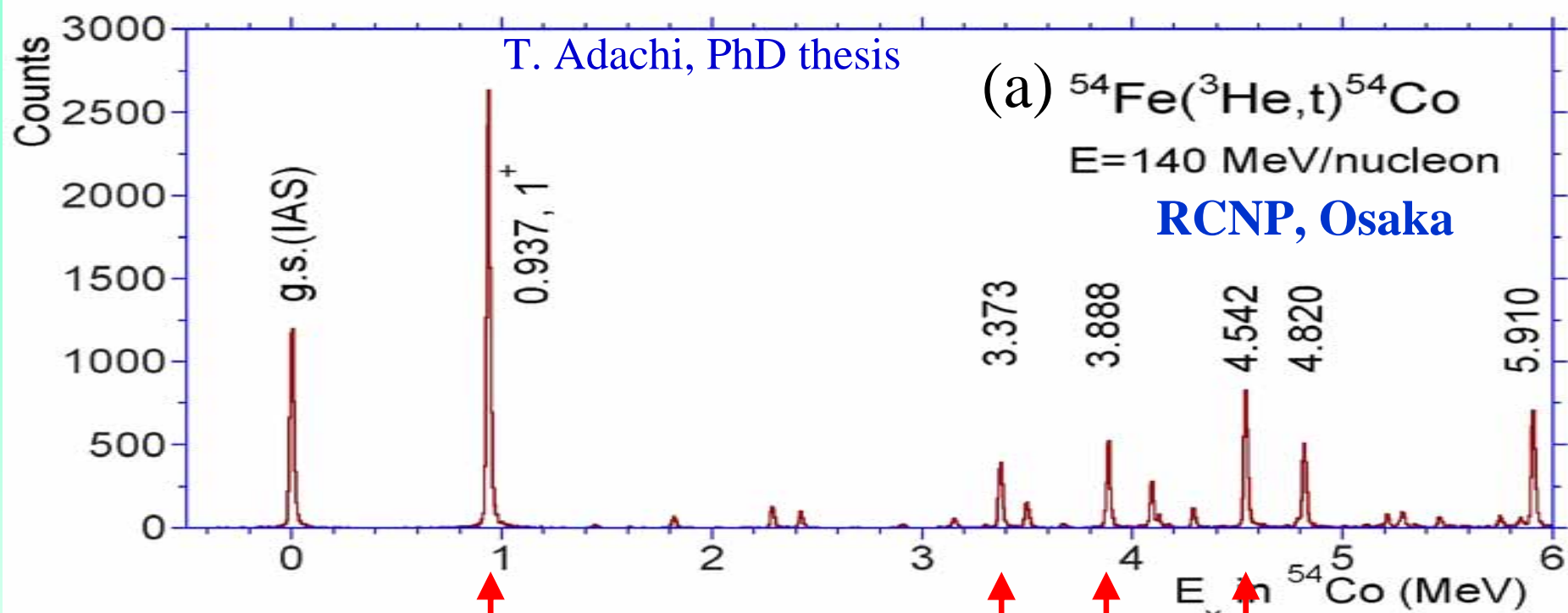
- at Louvain la Neuve (ISOL facility)

- at GSI (FRS facility)

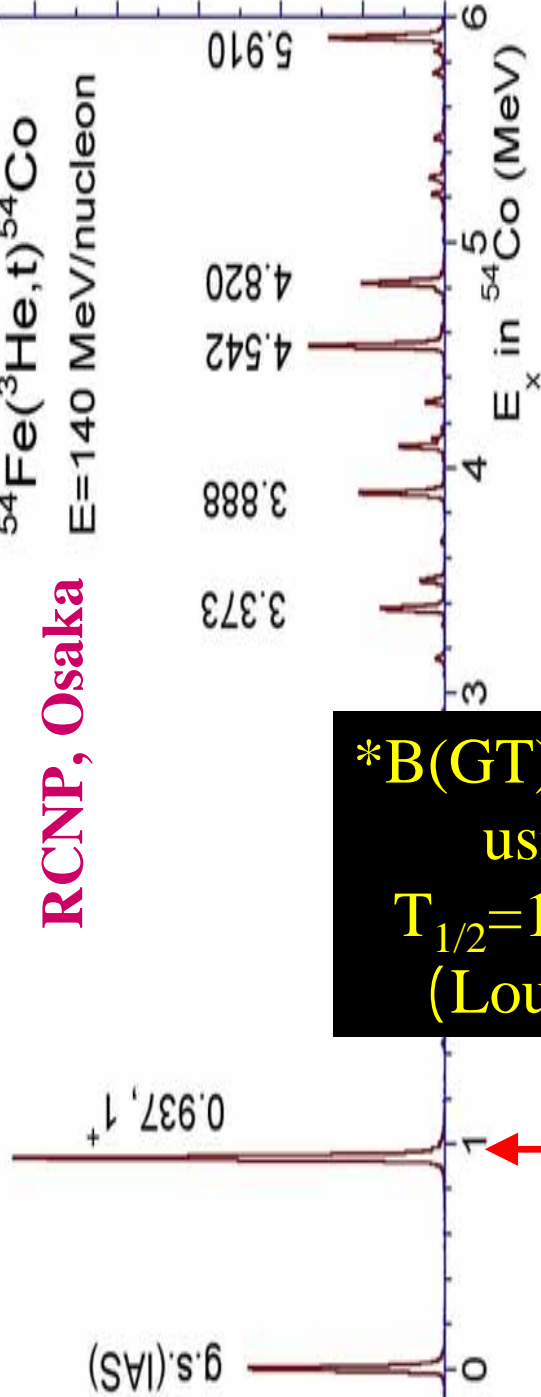


# GSI: RISING set up - active stopper campaign -





**RCNP, Osaka**  
 $^{54}\text{Fe}(^3\text{He}, t)^{54}\text{Co}$   
 $E=140\text{ MeV/nucleon}$



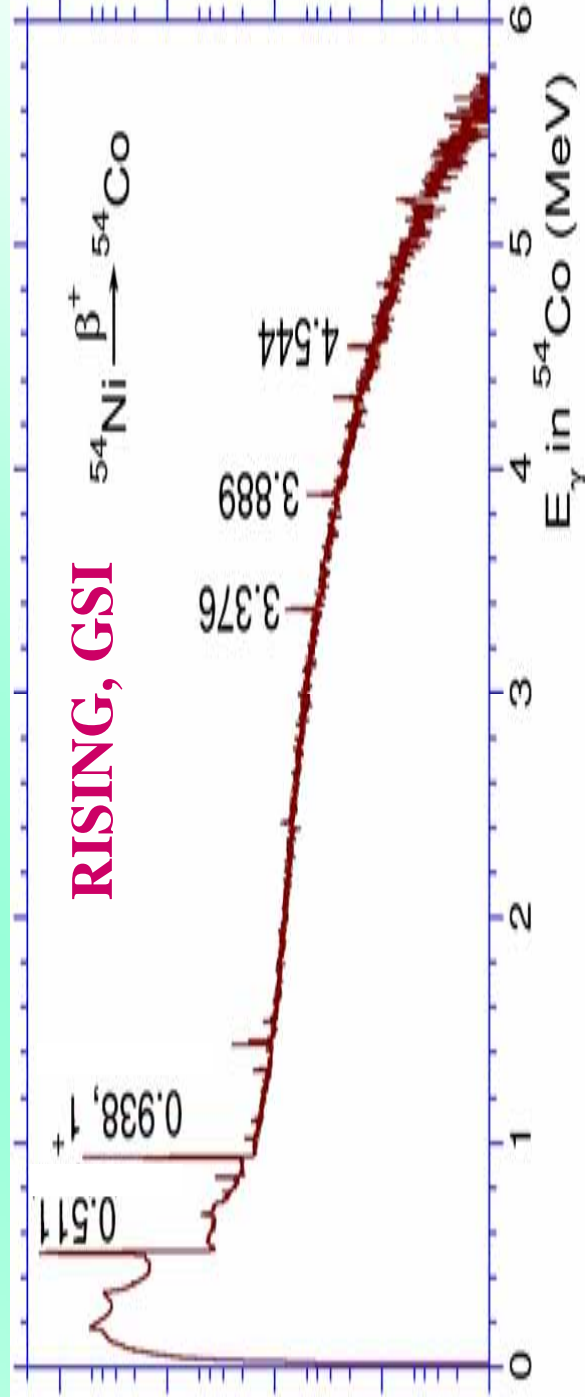
**\*B(GT) values  
 using  
 $T_{1/2}=115\text{ ms}$   
 (Louvain)**

**Comparison  
 $B(\text{GT})$   $B(\text{GT})$   
 $(^3\text{He}, t)$   $\beta\text{-decay}$**

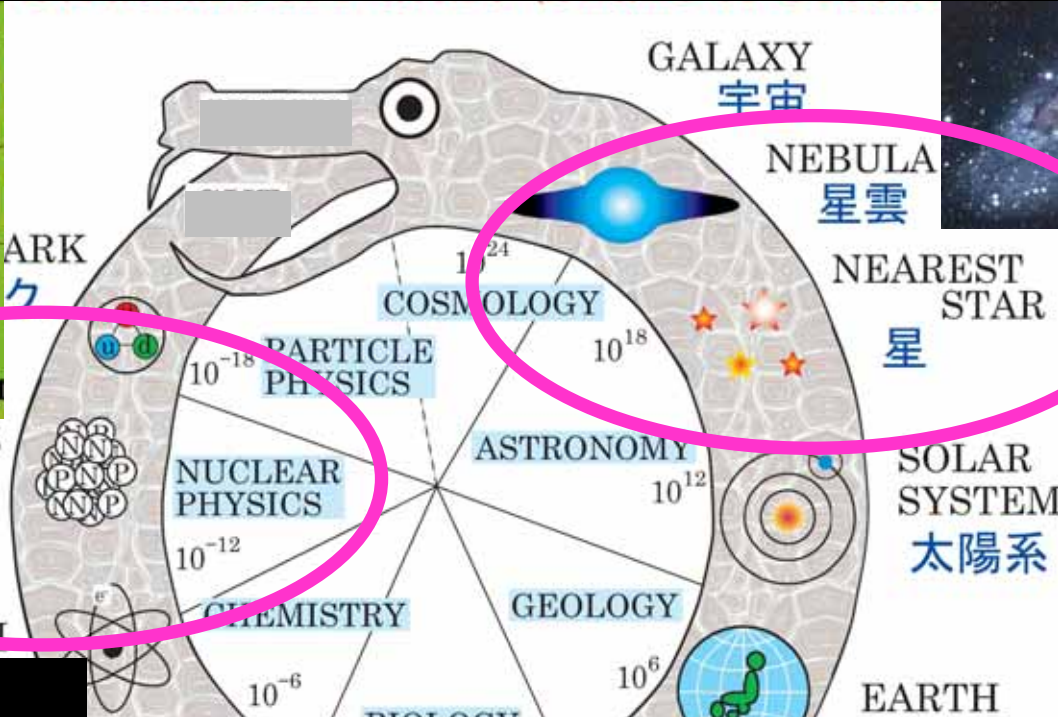
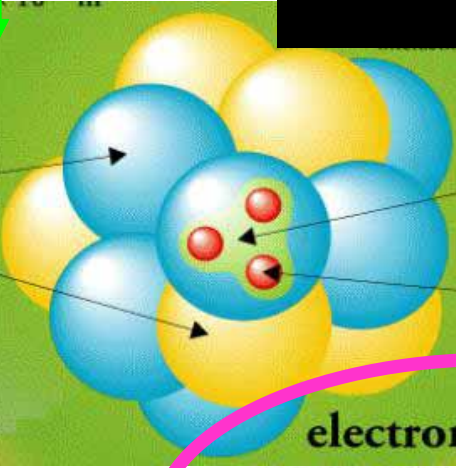
**0.09**  $\longleftrightarrow$  **0.07**  
**0.07**  $\longleftrightarrow$  **0.07**

**0.46**  $\longleftrightarrow$  **0.48**

**RISING, GSI**  
 $^{54}\text{Ni} \xrightarrow{\beta^+} ^{54}\text{Co}$



# The Layer Structure of the Nature (Snake of Uroboros)





# Summary

- \* **Weak response** of Nuclei was studied by using **Strong Int.**  
--Charge Exchange Reaction--
- \* **Isospin Symmetry** was introduced.
- \* **High resolution** of the ( $^3\text{He},t$ ) reaction  
allowed the comparison of analogous transitions
- \* **Absolute  $B(\text{GT})$  strengths** were derived.
- \* **High resolution** ( $p, p'$ ) and/or ( $^3\text{He}, ^3\text{He}'$ )  
allows the study of  $B(\text{E1})$  strengths.

**Extended Collaboration is very important!**